

# GPHY 5513

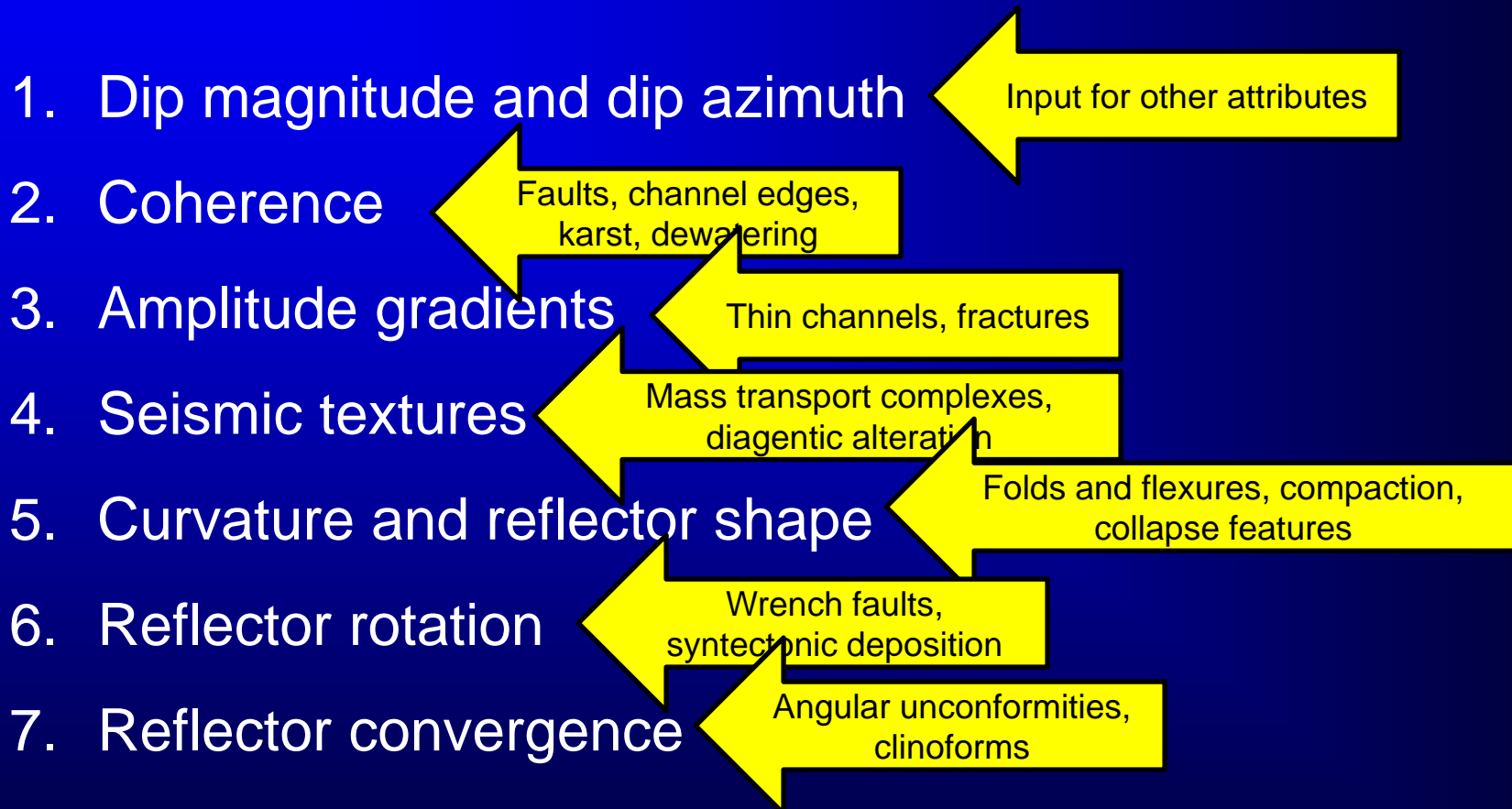
## 3D Seismic Interpretation

*Dr. Zonghu Liao*

### Volumetric Dip and Azimuth



# Geometric Attributes



# Volumetric dip and azimuth

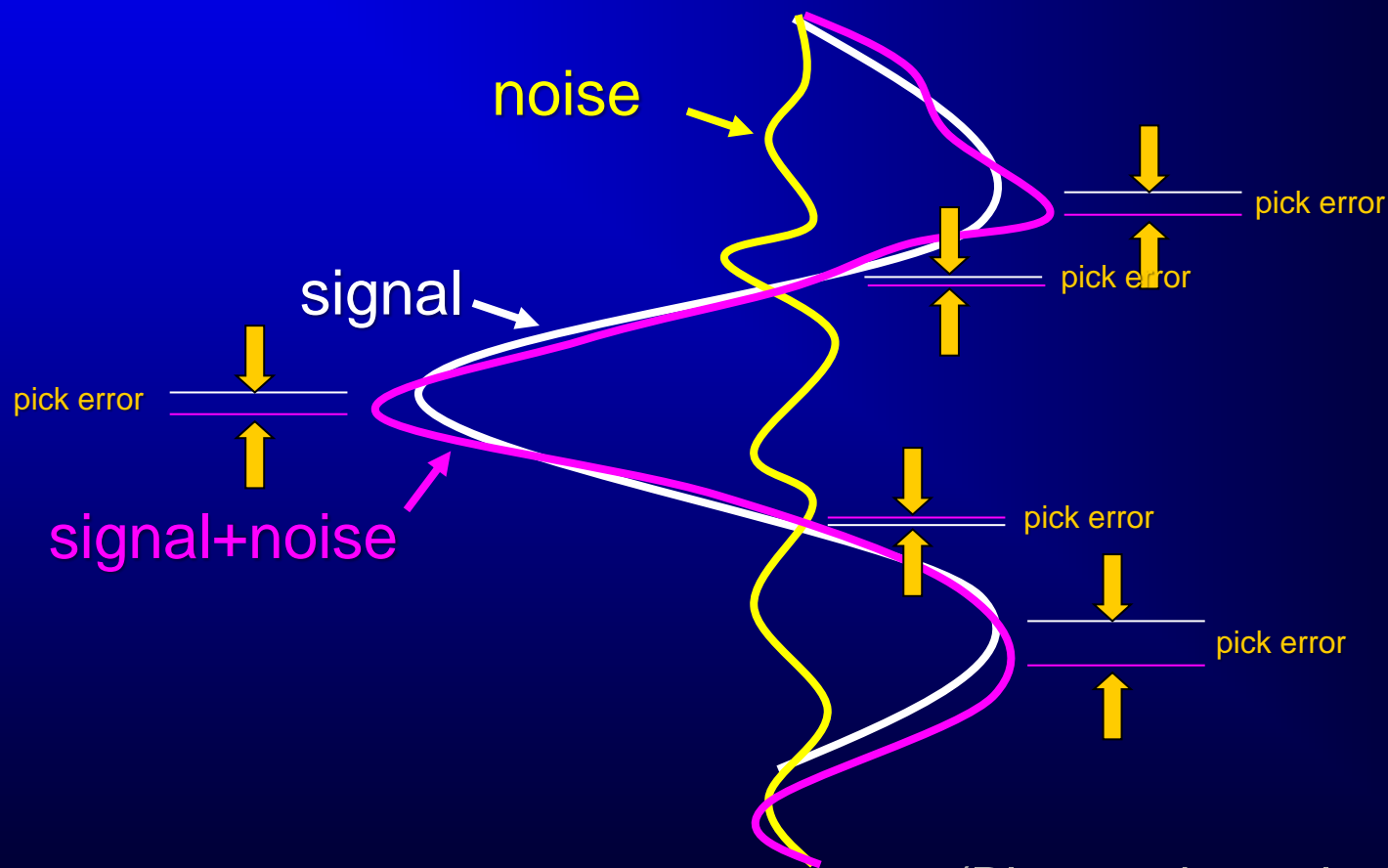
## After this section you will be able to:

- Evaluate alternative algorithms to calculate volumetric dip and azimuth in terms of accuracy and lateral resolution,
- Interpret shaded relief and apparent dip images to delineate subtle structural features, and
- Apply composite dip/azimuth/seismic images to determine how a given reflector dips in and out of the plane of view.



# Dip computed from picked maps:

Zero-crossing picks are less sensitive to noise than peaks or troughs



(Blumentritt et al., 2005)

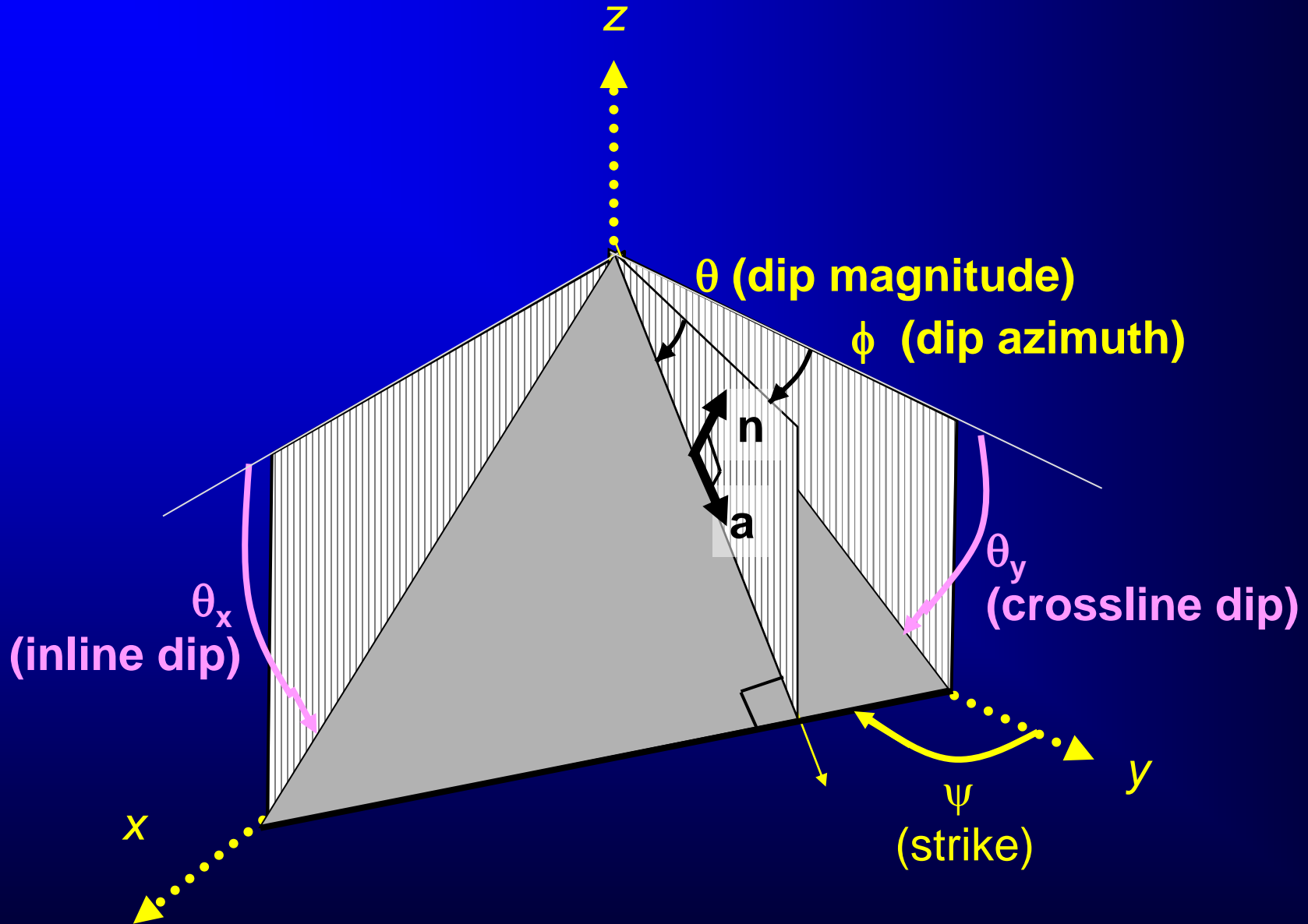


# Alternative volumetric measures of reflector dip and azimuth

1. 3D Complex trace analysis
2. Gradient Structure Tensor (GST)
3. Plane-wave destructor
4. Discrete scans for dip of most coherent reflector



# Definition of reflector dip



# 1. 3D Complex Trace Analysis (Instantaneous Dip/Azimuth)

Instantaneous phase

$$\phi = \text{ATAN2}(d^H, d)$$

Hilbert transform

Instantaneous frequency

$$\omega = 2\pi f = 2\pi \frac{\partial \phi}{\partial t} = 2\pi \frac{\frac{\partial d^H}{\partial t} d - \frac{\partial d}{\partial t} d^H}{d^2 + (d^H)^2}$$

Instantaneous  
in line wavenumber

$$k_x = \frac{\partial \phi}{\partial x} = \frac{\frac{\partial d^H}{\partial x} d - \frac{\partial d}{\partial x} d^H}{d^2 + (d^H)^2}$$

Instantaneous  
cross line wavenumber

$$k_y = \frac{\partial \phi}{\partial y} = \frac{\frac{\partial d^H}{\partial y} d - \frac{\partial d}{\partial y} d^H}{d^2 + (d^H)^2}$$

Instantaneous  
apparent dips

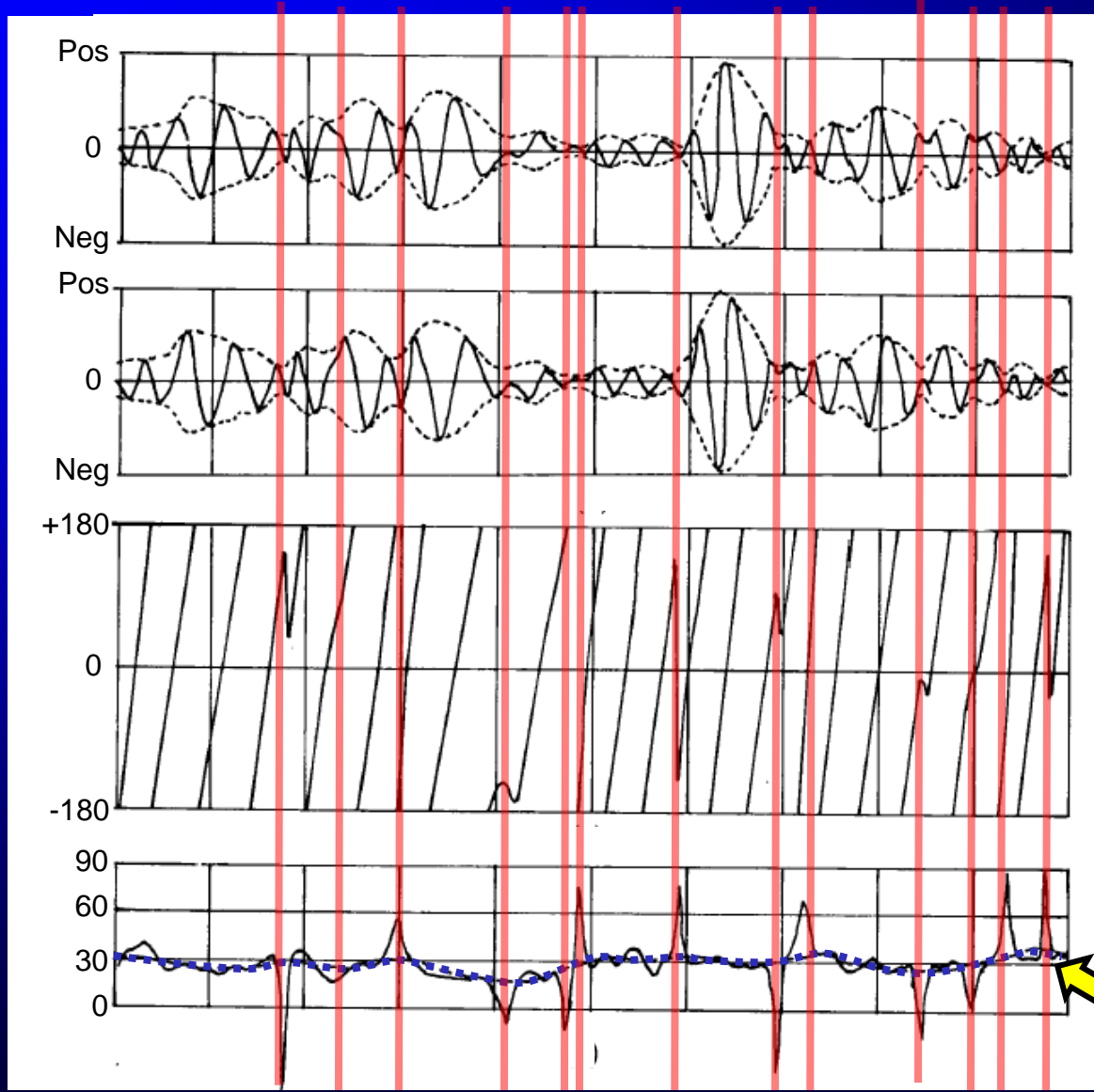
$$p = \frac{k_x}{\omega}; q = \frac{k_y}{\omega}$$

$$s = \sqrt{p^2 + q^2}$$

$$\psi = \text{ATAN2}(q, p)$$

# The analytic trace

Original data (real component)  
 Quadrature (imaginary component)  
 Phase  
 Frequency (Hz)



$d(t)$

$d^H(t)$

$$\phi(t) = \text{ATAN2}[d^H(t), d(t)]$$

$$\bar{f}_n \equiv \frac{\sum_{k=-K}^K e_{n+k} f_{n+k}}{\sum_{k=-K}^K e_{n+k}}$$

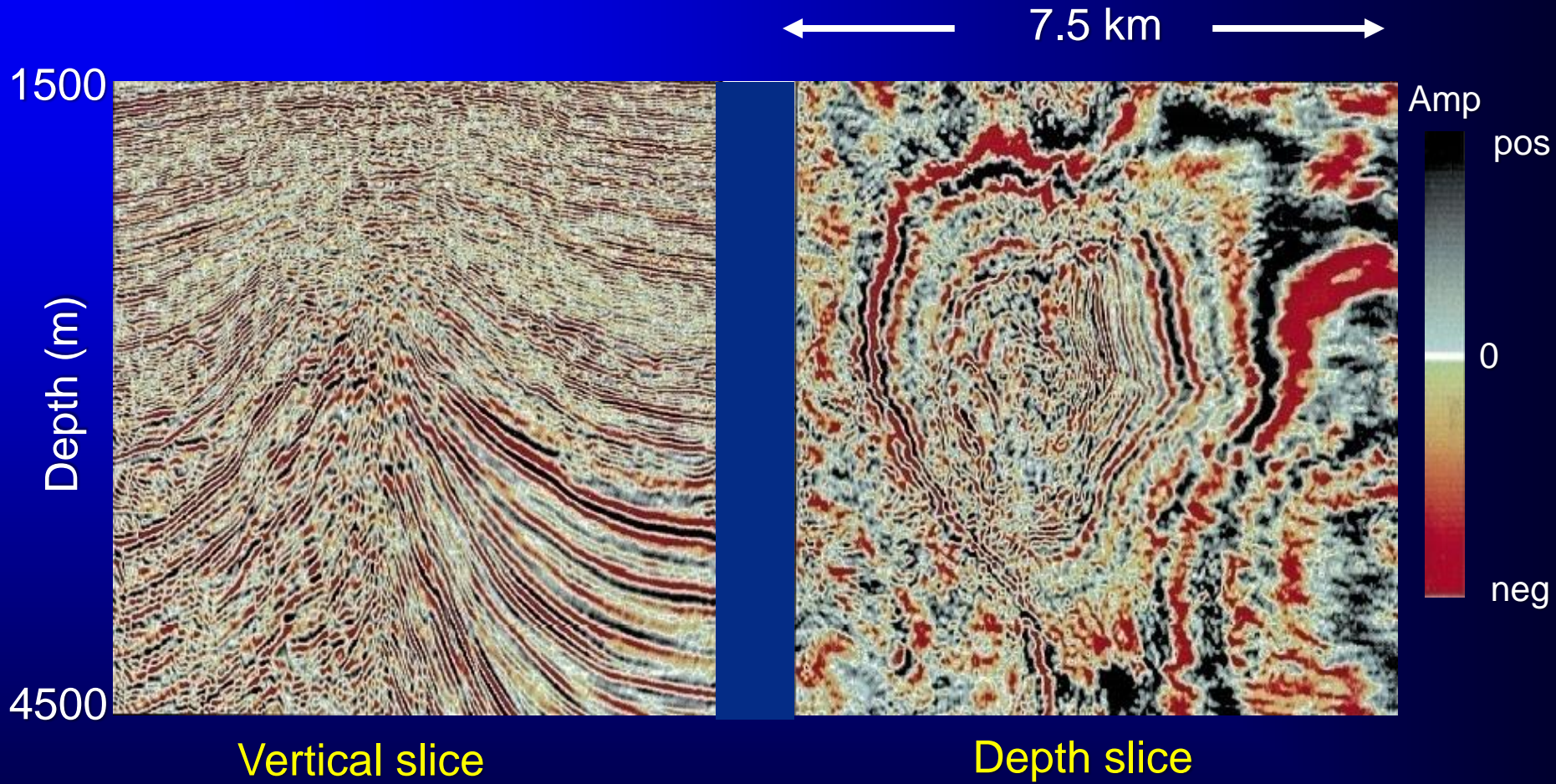
Weighted-average frequency

(Taner et al., 1979)





# Seismic data



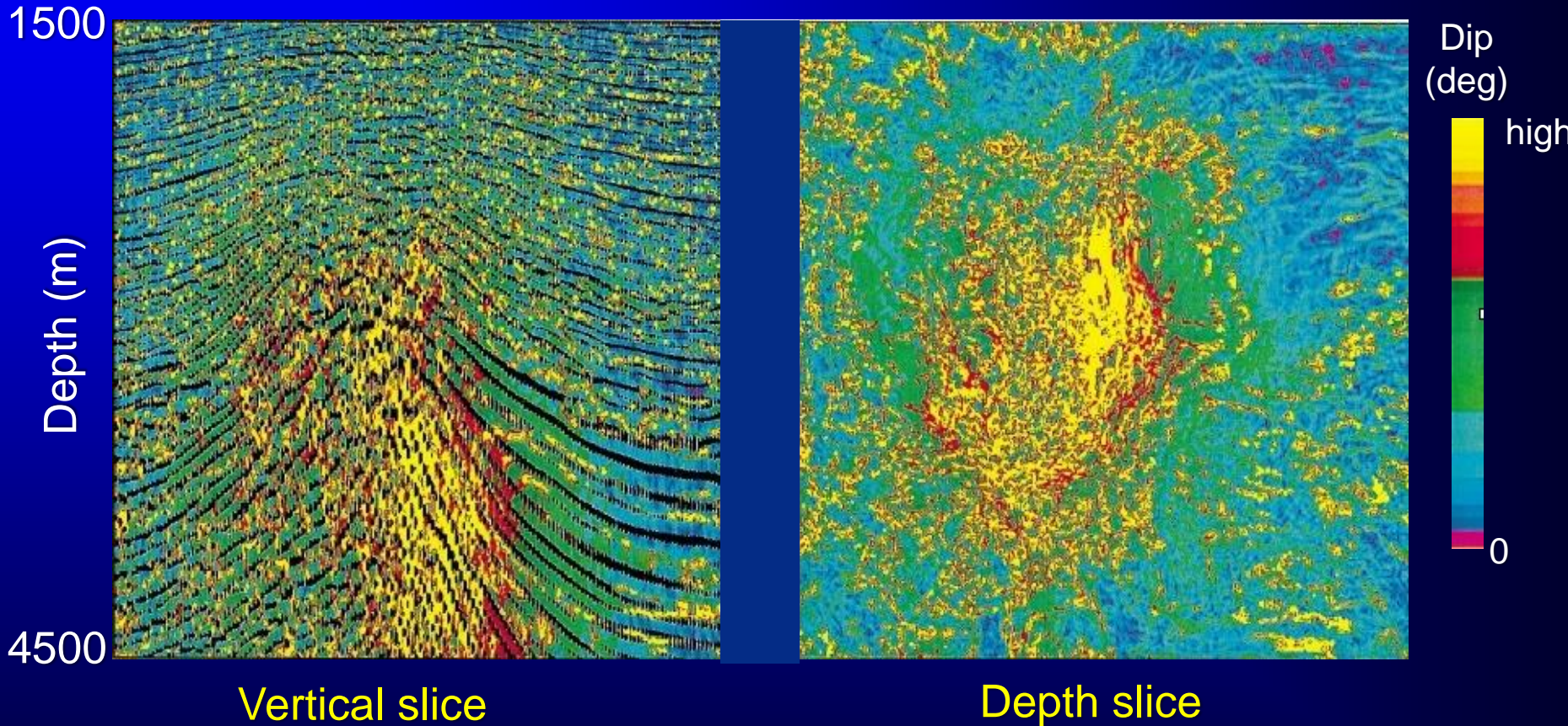
(Barnes, 2000)



# Instantaneous dip magnitude (sensitive to errors in $\omega$ , $k_x$ and $k_y$ !)

$$s = \sqrt{p^2 + q^2}$$

← 7.5 km →



(Barnes, 2000)

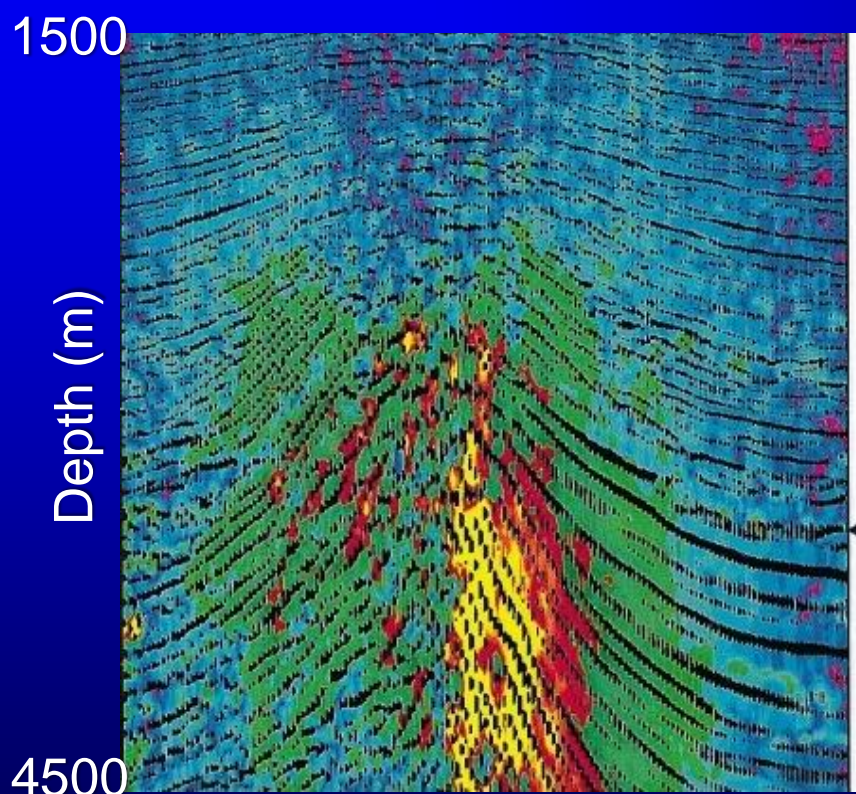


# Weighted average dip magnitude

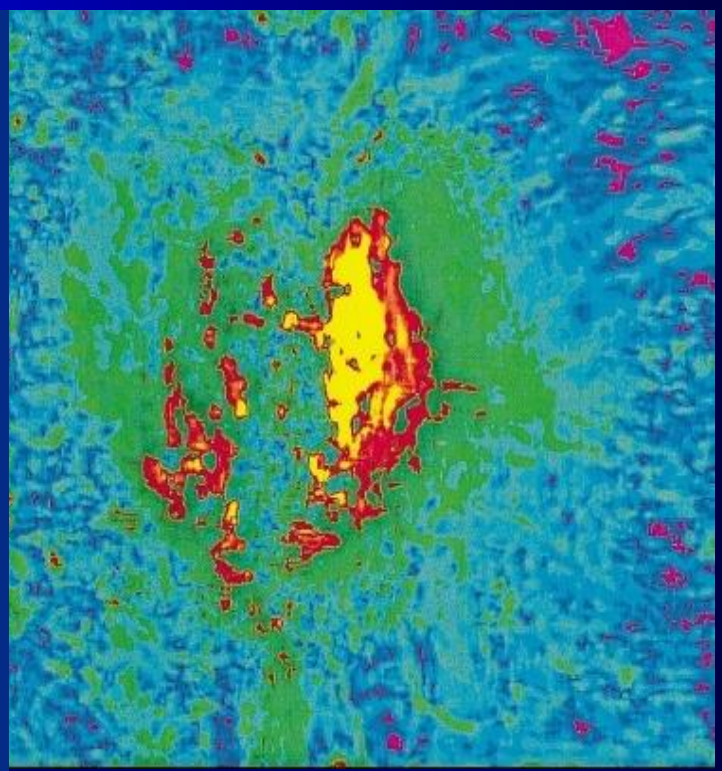
(5 crossline by 5 inline by 7 sample window)

$$\bar{s} = \sqrt{\left(\frac{\overline{k_x}}{\omega}\right)^2 + \left(\frac{\overline{k_y}}{\omega}\right)^2}$$

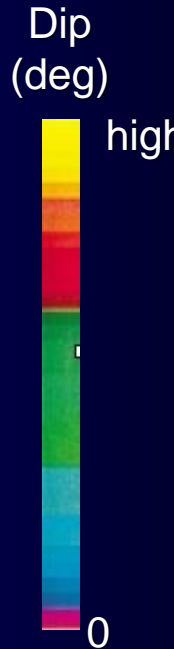
← 7.5 km →



Vertical slice



Depth slice

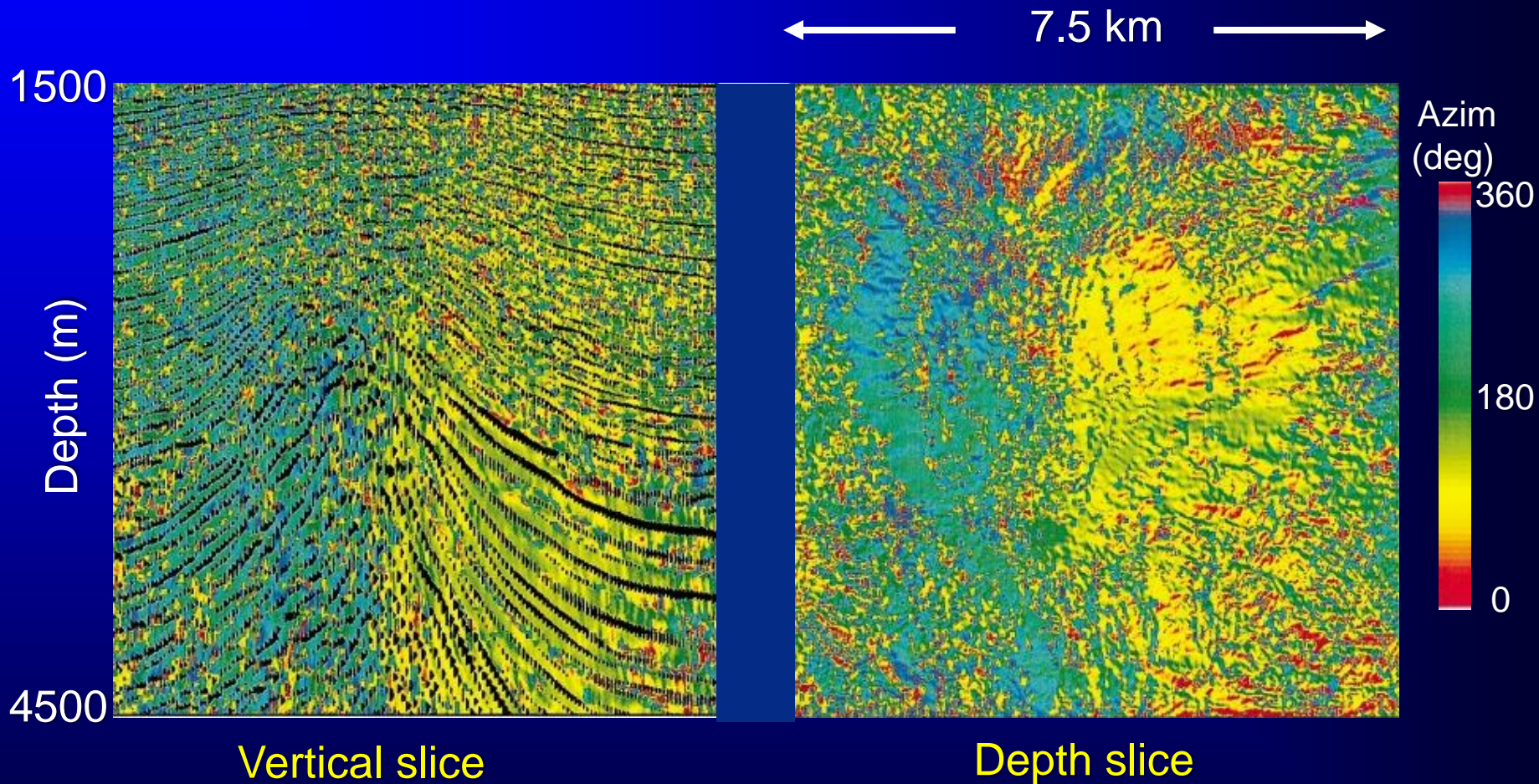


$$\bar{\omega}_{rst} \equiv \frac{\sum_{l=-L}^{+L} \sum_{k=-K}^{+K} \sum_{j=-J}^{+J} e_{r+j, s+k, t+l} \omega_{r+j, s+k, t+l}}{\sum_{l=-L}^{+L} \sum_{k=-K}^{+K} \sum_{j=-J}^{+J} e_{r+j, s+k, t+l}}$$



# Instantaneous dip azimuth

$$\psi = \text{ATAN2}(q, p)$$

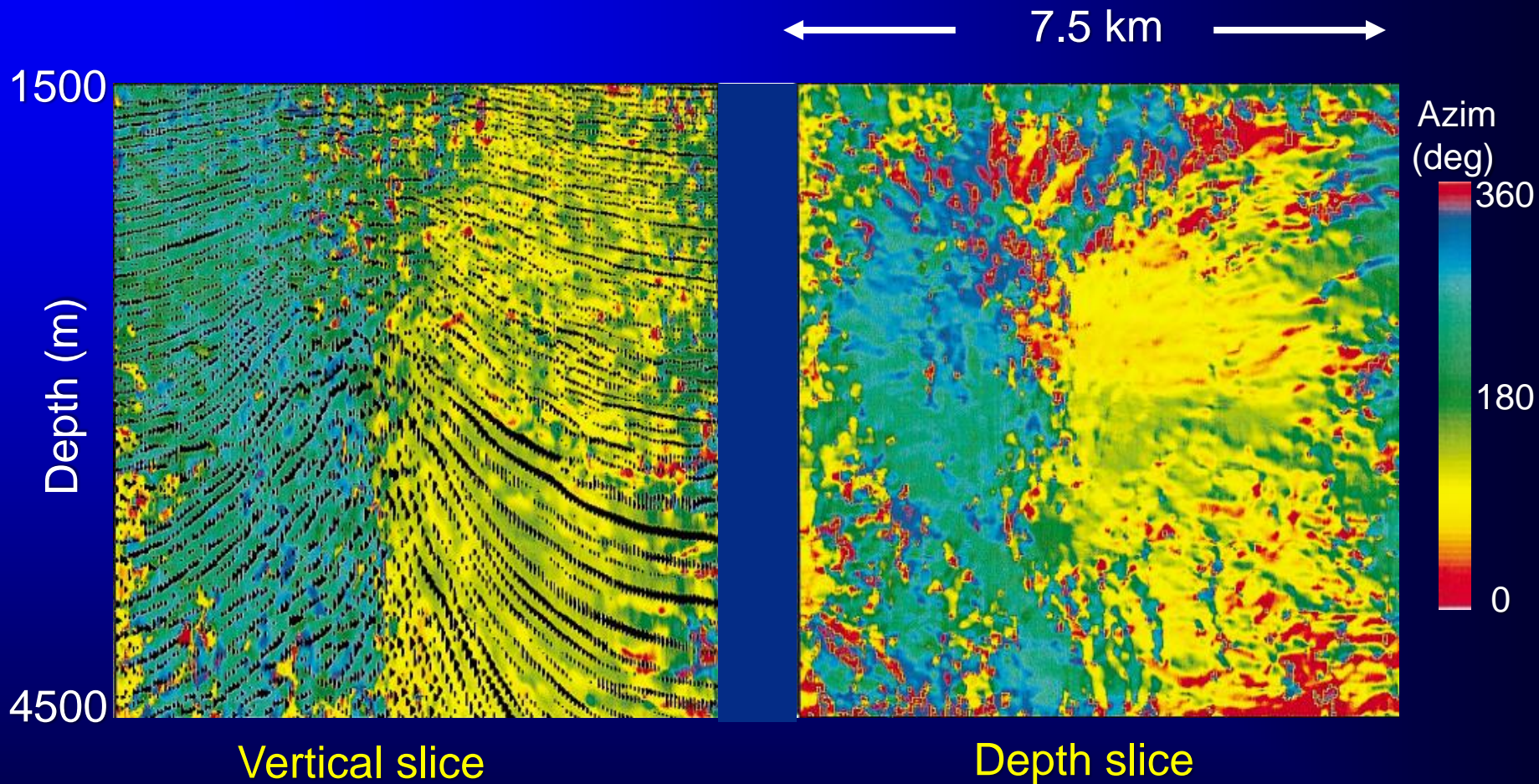




# Weighted average dip azimuth

(5 crossline by 5 inline by 7 sample window)

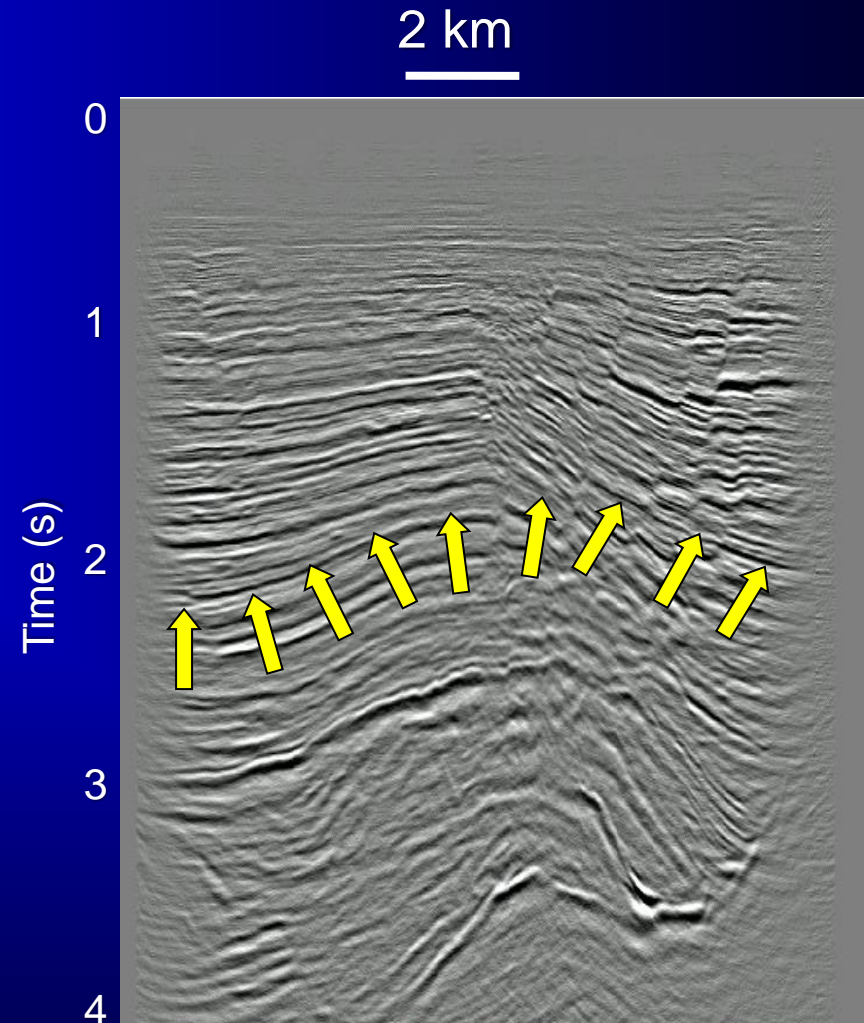
$$\bar{\psi} = \text{ATAN2} \left( \frac{\bar{k}_y}{\bar{\omega}}, \frac{\bar{k}_x}{\bar{\omega}} \right)$$



## 2. Gradient Structure Tensor (GST)

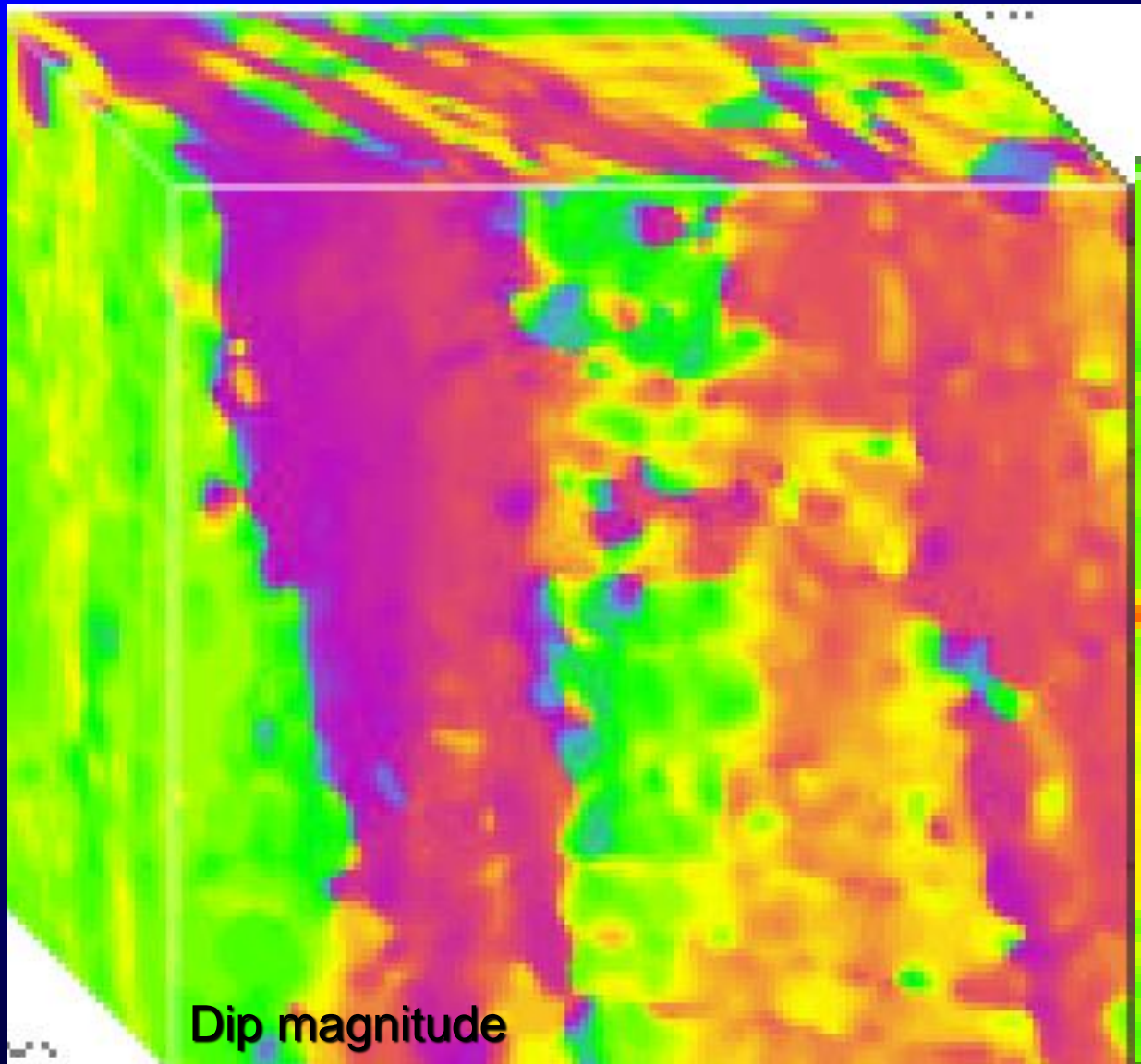
$$\mathbf{T}_{\text{GS}} = \begin{bmatrix} \left\langle \frac{\partial u}{\partial x} \frac{\partial u}{\partial x} \right\rangle & \left\langle \frac{\partial u}{\partial y} \frac{\partial u}{\partial x} \right\rangle & \left\langle \frac{\partial u}{\partial z} \frac{\partial u}{\partial x} \right\rangle \\ \left\langle \frac{\partial u}{\partial x} \frac{\partial u}{\partial y} \right\rangle & \left\langle \frac{\partial u}{\partial y} \frac{\partial u}{\partial y} \right\rangle & \left\langle \frac{\partial u}{\partial z} \frac{\partial u}{\partial y} \right\rangle \\ \left\langle \frac{\partial u}{\partial x} \frac{\partial u}{\partial z} \right\rangle & \left\langle \frac{\partial u}{\partial y} \frac{\partial u}{\partial z} \right\rangle & \left\langle \frac{\partial u}{\partial z} \frac{\partial u}{\partial z} \right\rangle \end{bmatrix}$$

The eigenvector of the  $\mathbf{T}_{\text{GS}}$  matrix points in the direction of the maximum amplitude gradient





## 2. Gradient Structure Tensor (GST)



### 3. Plane-wave destructor

Predict a trace  $s_j$ , from a neighboring trace along an unknown inline dip,  $p$ :

$$s_j(t) \approx s_{j-1}(t + px) \equiv P_{j,j-1}^{(x)}(p)s_{j-1}(t)$$

Minimize the squared error,  $\epsilon^2$ , along the inline dip direction,  $p$ :

$$\|\boldsymbol{\epsilon}\|^2 \equiv \sum_{j=2}^J \|s_j - s_{j-1}(t + px)\|^2 = \|\mathbf{D}\mathbf{s}\|^2$$

$$\mathbf{D} = \begin{bmatrix} \mathbf{I} & 0 & 0 & \dots & 0 \\ -\mathbf{P}_{1,2} & \mathbf{I} & 0 & \dots & 0 \\ 0 & -\mathbf{P}_{2,3} & \mathbf{I} & \dots & 0 \\ \dots & \dots & \dots & \dots & \dots \\ 0 & 0 & \dots & -\mathbf{P}_{N-1,N} & \mathbf{I} \end{bmatrix}$$





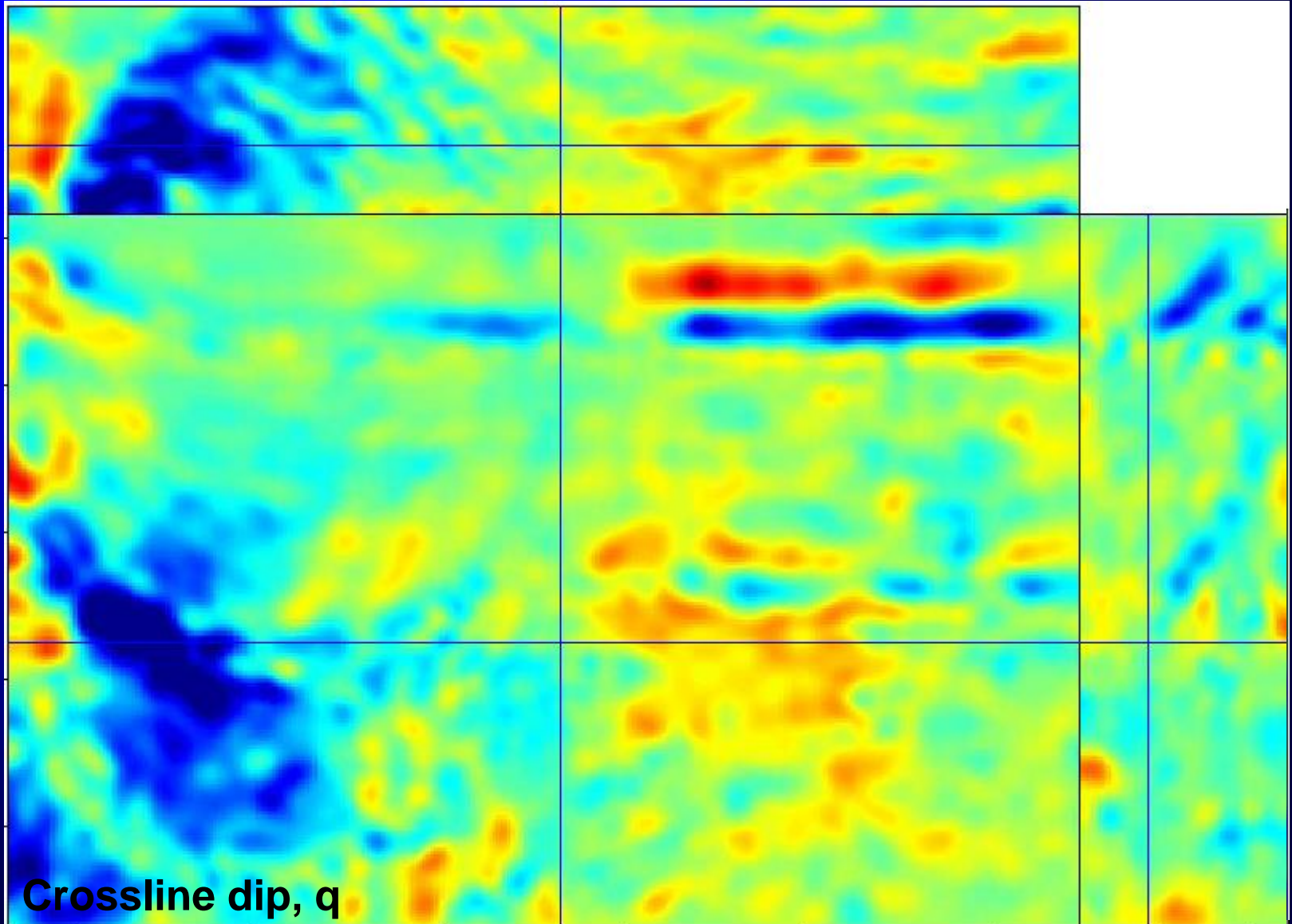
### 3. Plane-wave destructor (using Marfurt's inelegant math)

1. Predict (interpolate) the adjacent trace at unknown sample  $t+px$  using a simple 3-point parabola

$$\begin{aligned} s_j(t + px) \approx & s_{j-1}(t) \\ & + \frac{s_{j-1}(t + \Delta t) - s_{j-1}(t - \Delta t)}{2\Delta t} (px) \\ & + \frac{s_{j-1}(t + \Delta t) - 2s_{j-1}(t) + s_{j-1}(t - \Delta t)}{(\Delta t)^2} (px)^2 \end{aligned}$$

2. Minimize the predicted error by minimizing the objective function with respect to  $p$ .

### 3. Plane-wave destructor

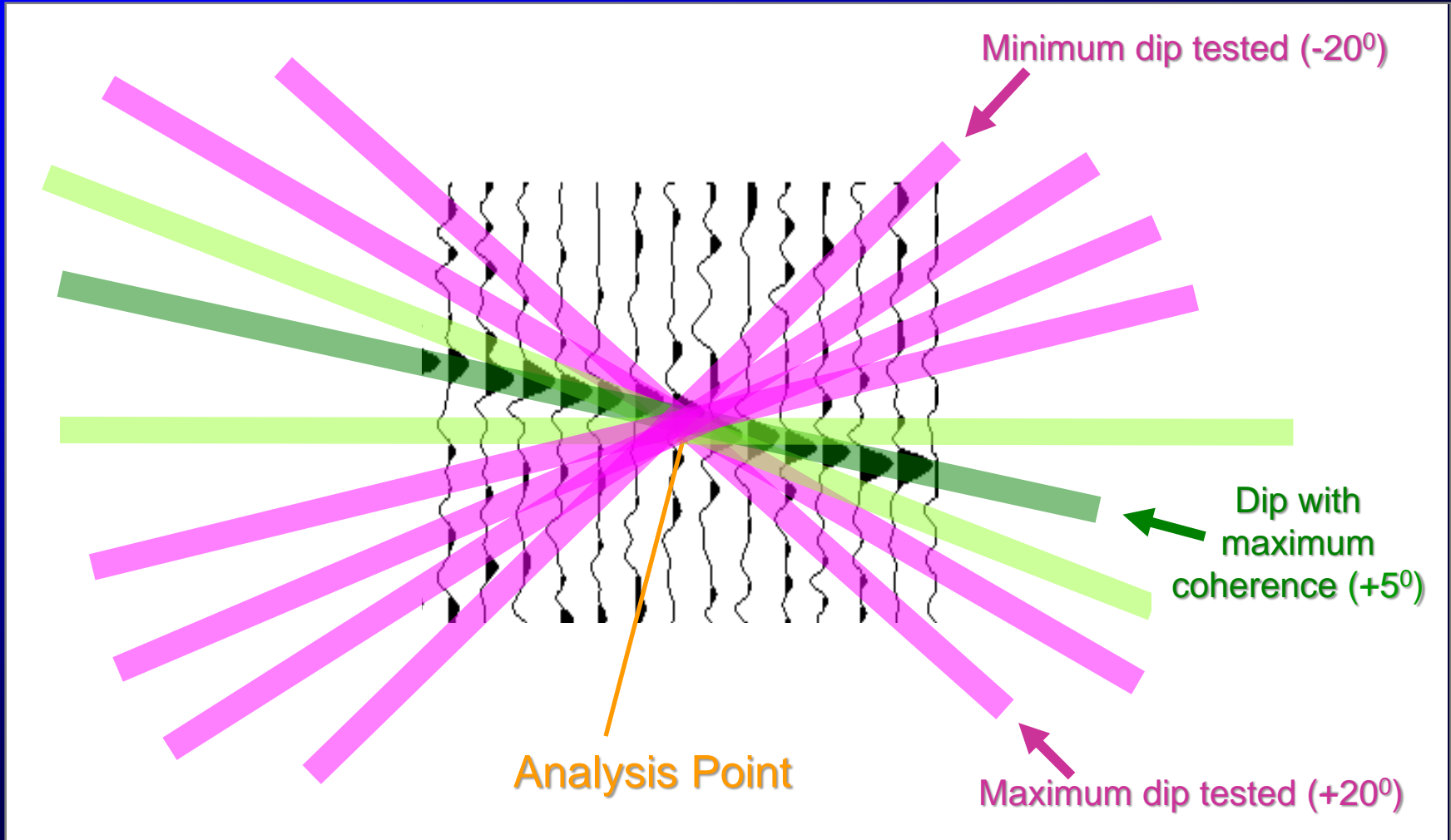


Crossline dip,  $q$



(Fomel, 2008)

## 4. Discrete scans for dip of most coherent reflector

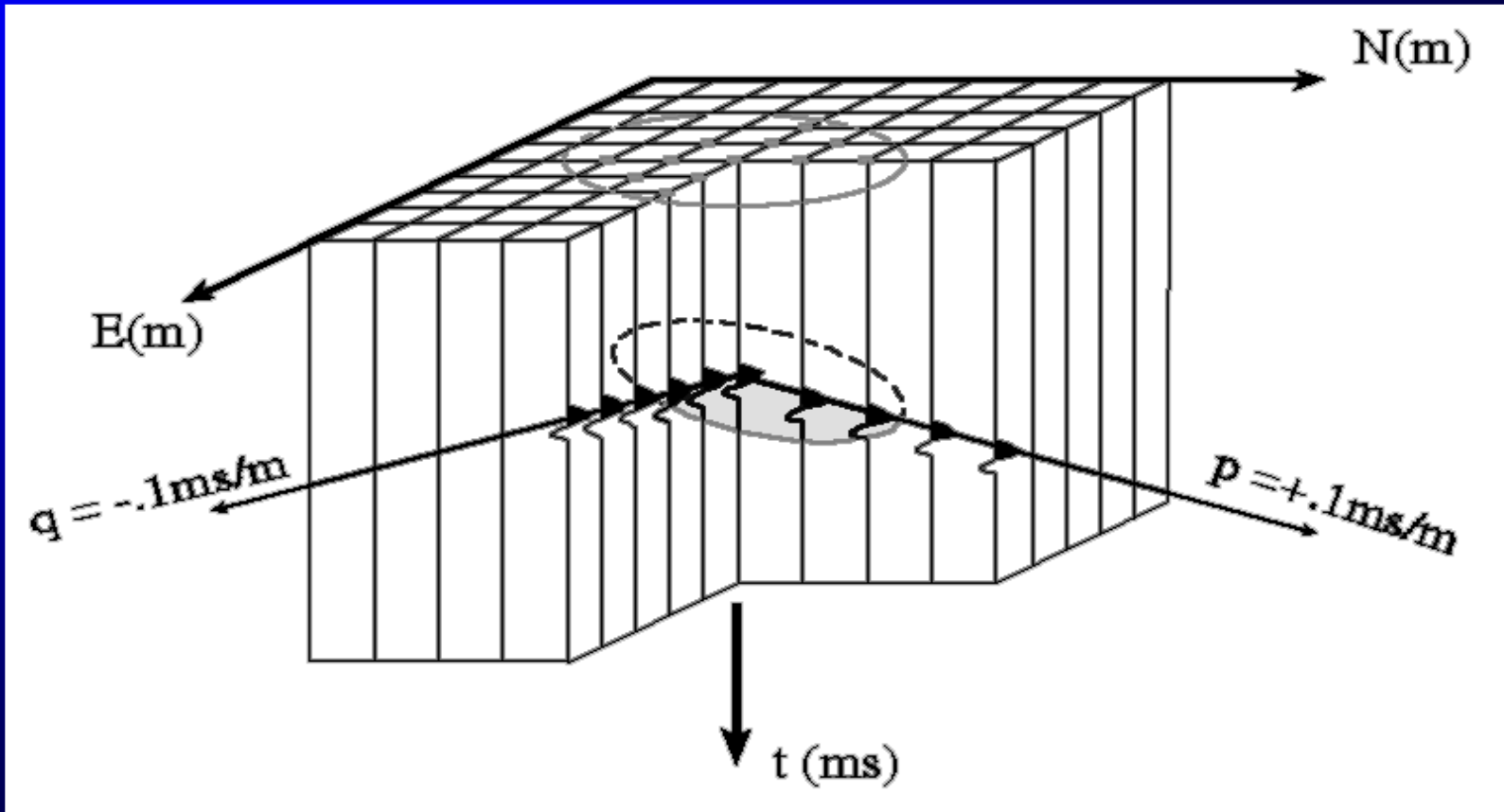


Instantaneous dip = dip with highest coherence

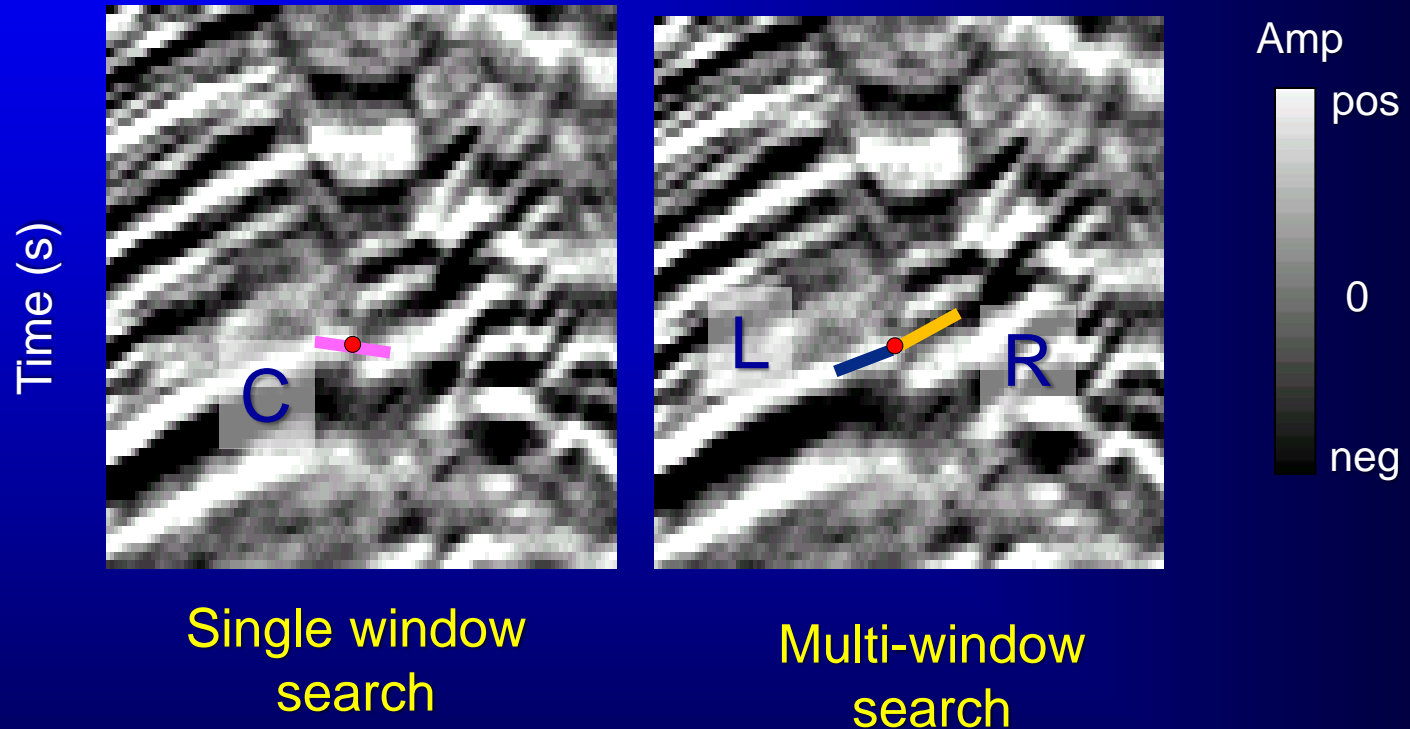
(Marfurt et al, 1998)



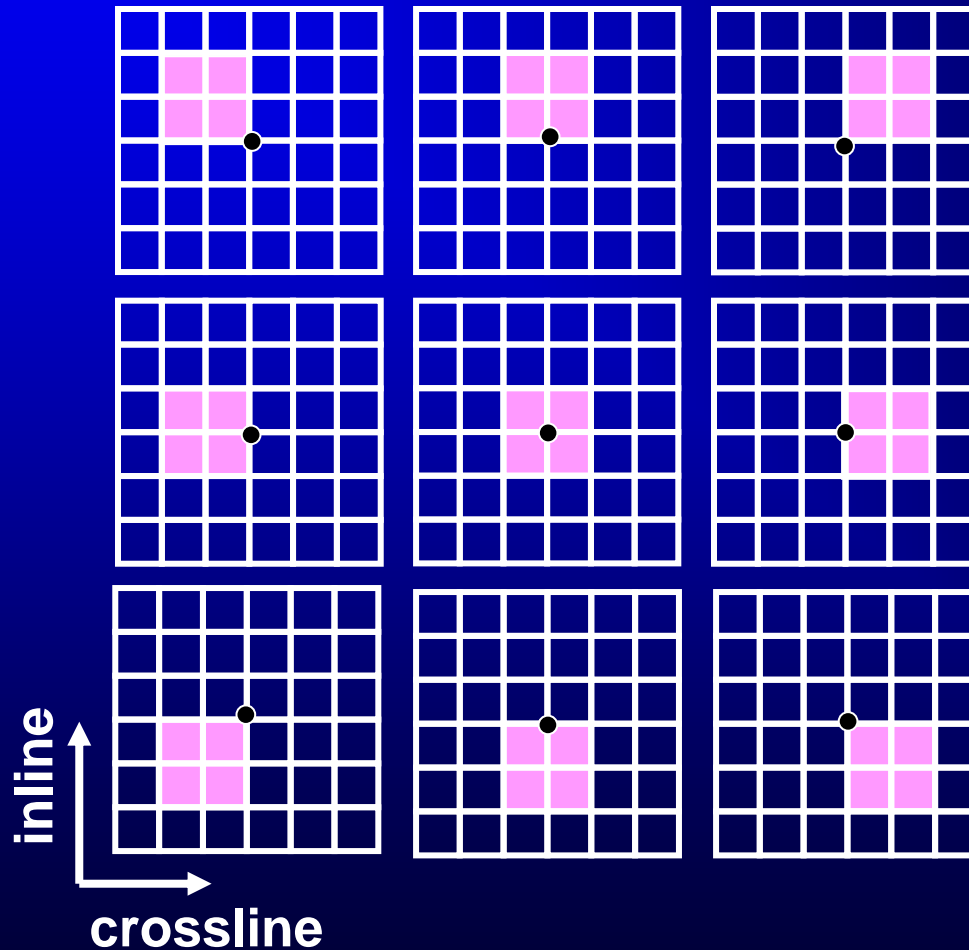
# 3D estimate of coherence and dip/azimuth



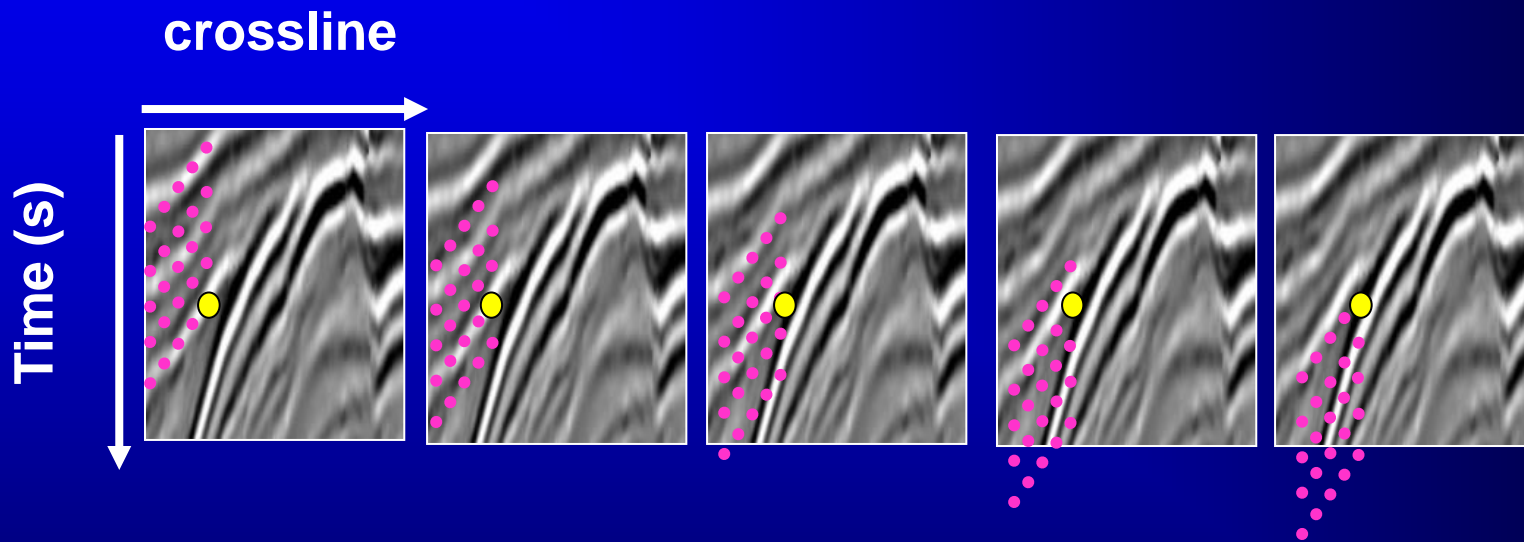
# Searching for dip in the presence of faults



# Search for the most coherent window containing the analysis point



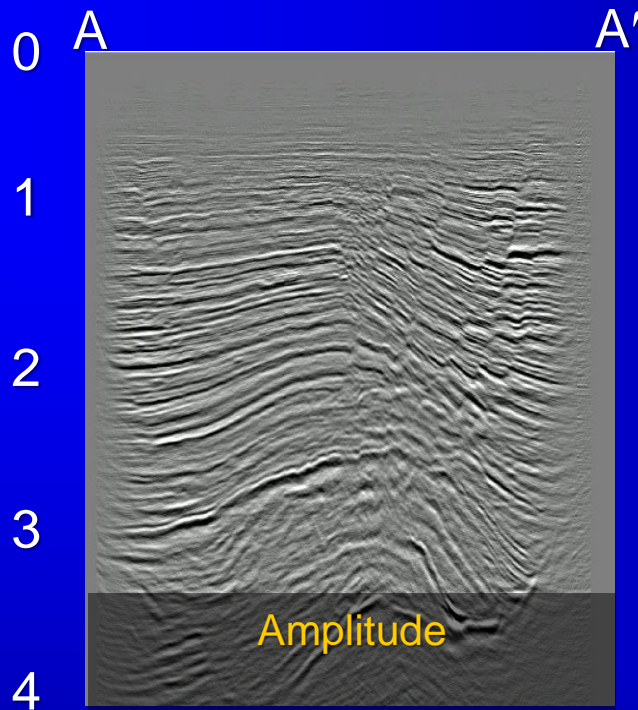
# Search for the most coherent window containing the analysis point



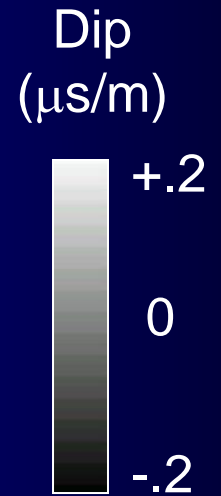
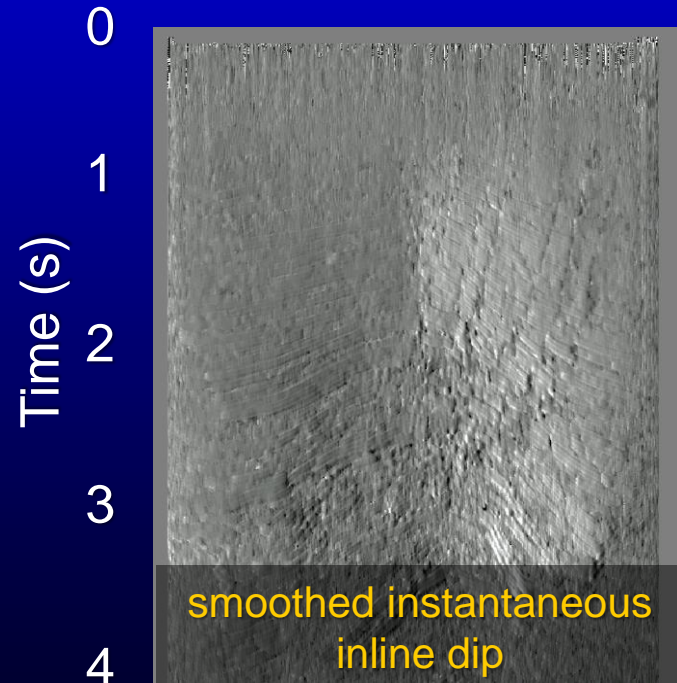


2 km

Time (s)



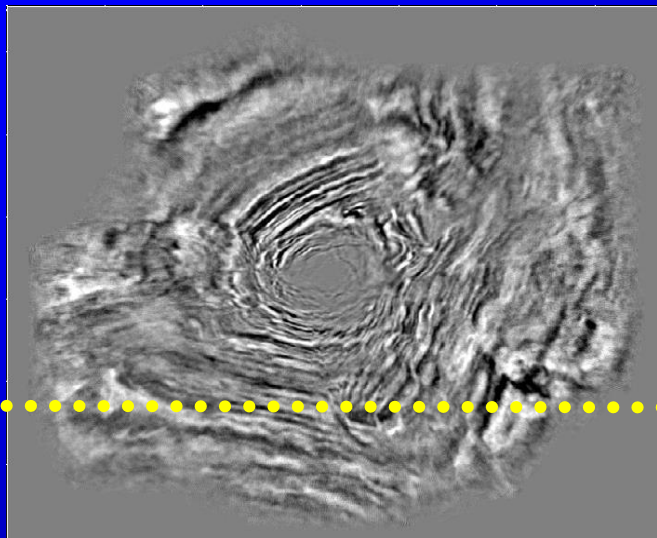
Comparison of dip estimates on vertical slice



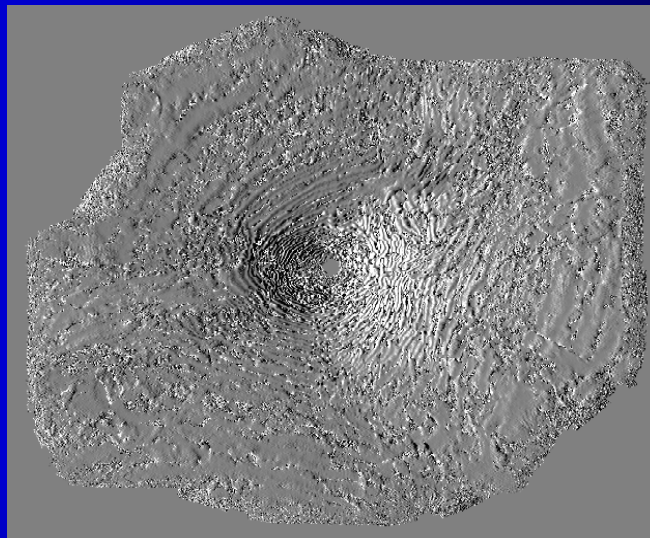
(Marfurt, 2008)



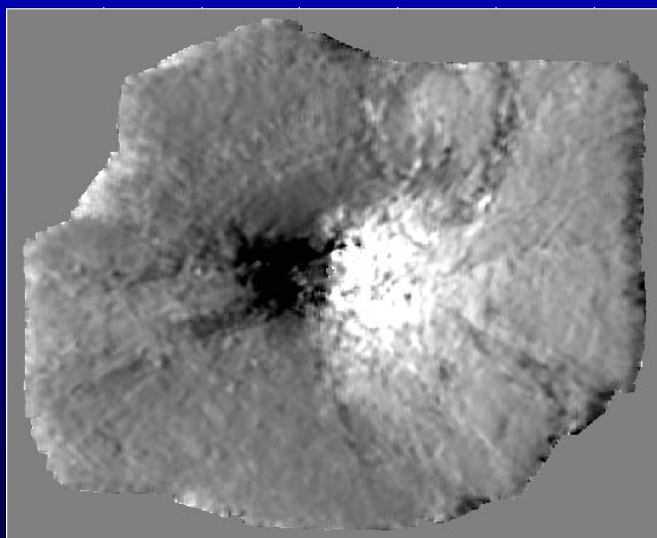
2 km



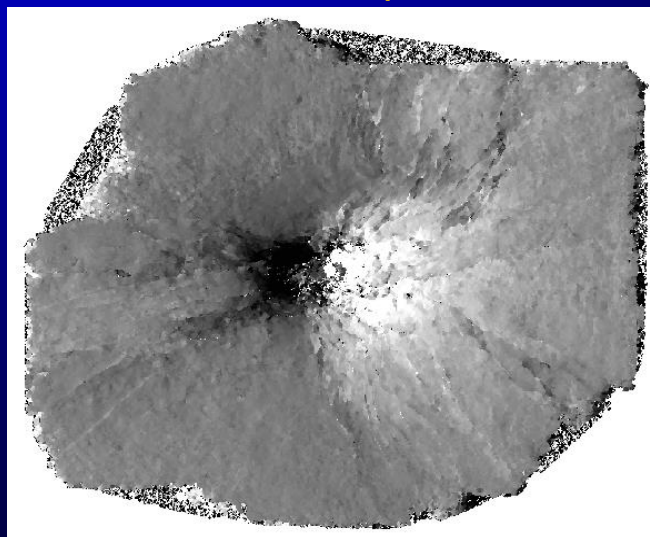
Amplitude



simple instantaneous inline dip



smoothed instantaneous inline dip



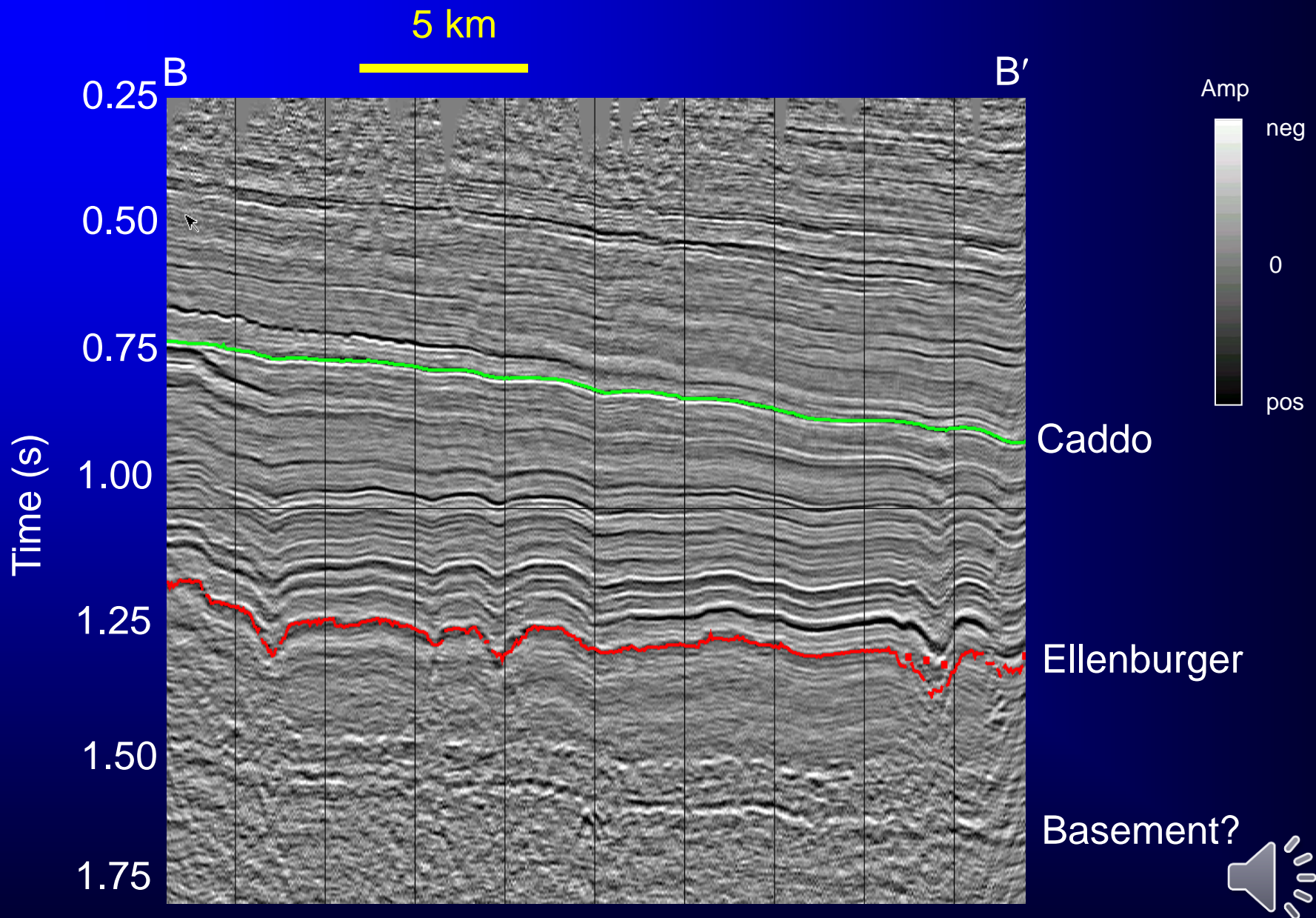
multi-window scan of inline dip

Comparison of dip estimates on time slice (t=1.0 s)



(Marfurt, 2008)

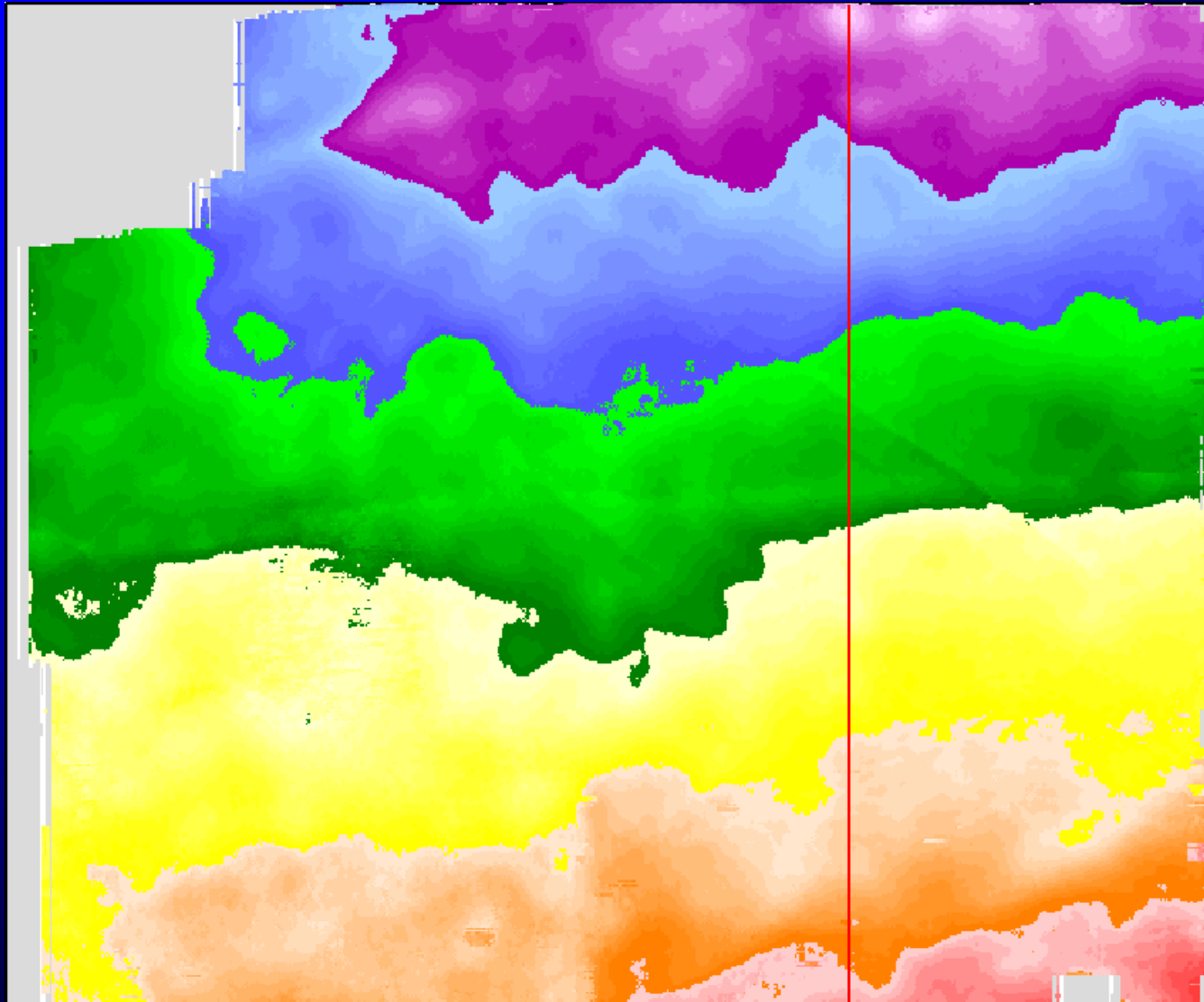
# Vertical Slice through Seismic



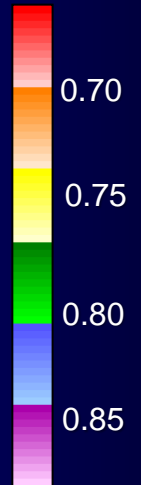
# Time/structure of Caddo horizon

5 km

B'



Time (s)



B

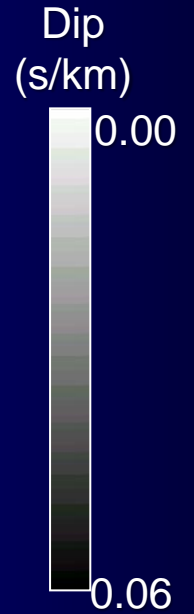
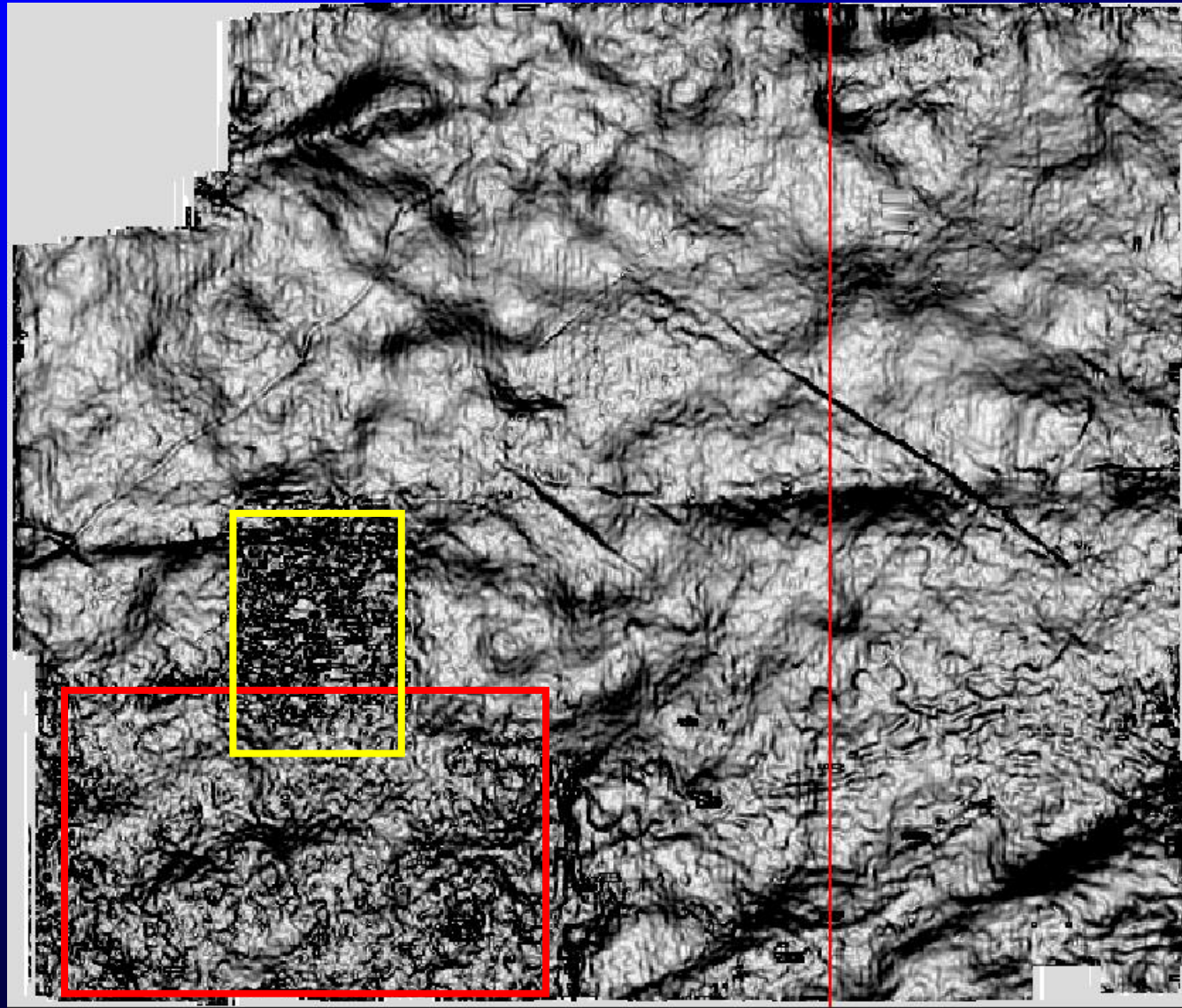




# Dip magnitude from picked Caddo horizon

5 km

B'



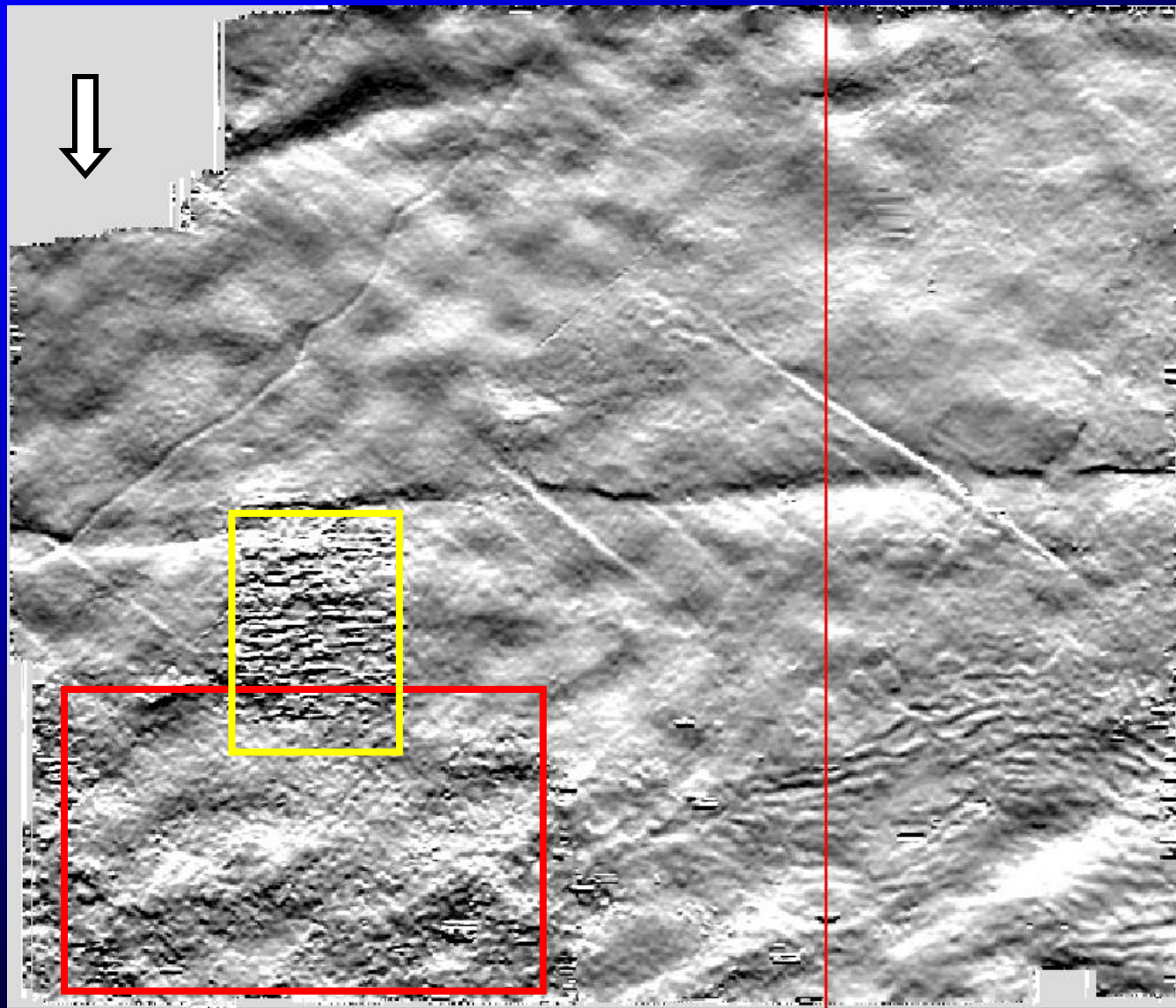
B



# NS dip from picked Caddo horizon

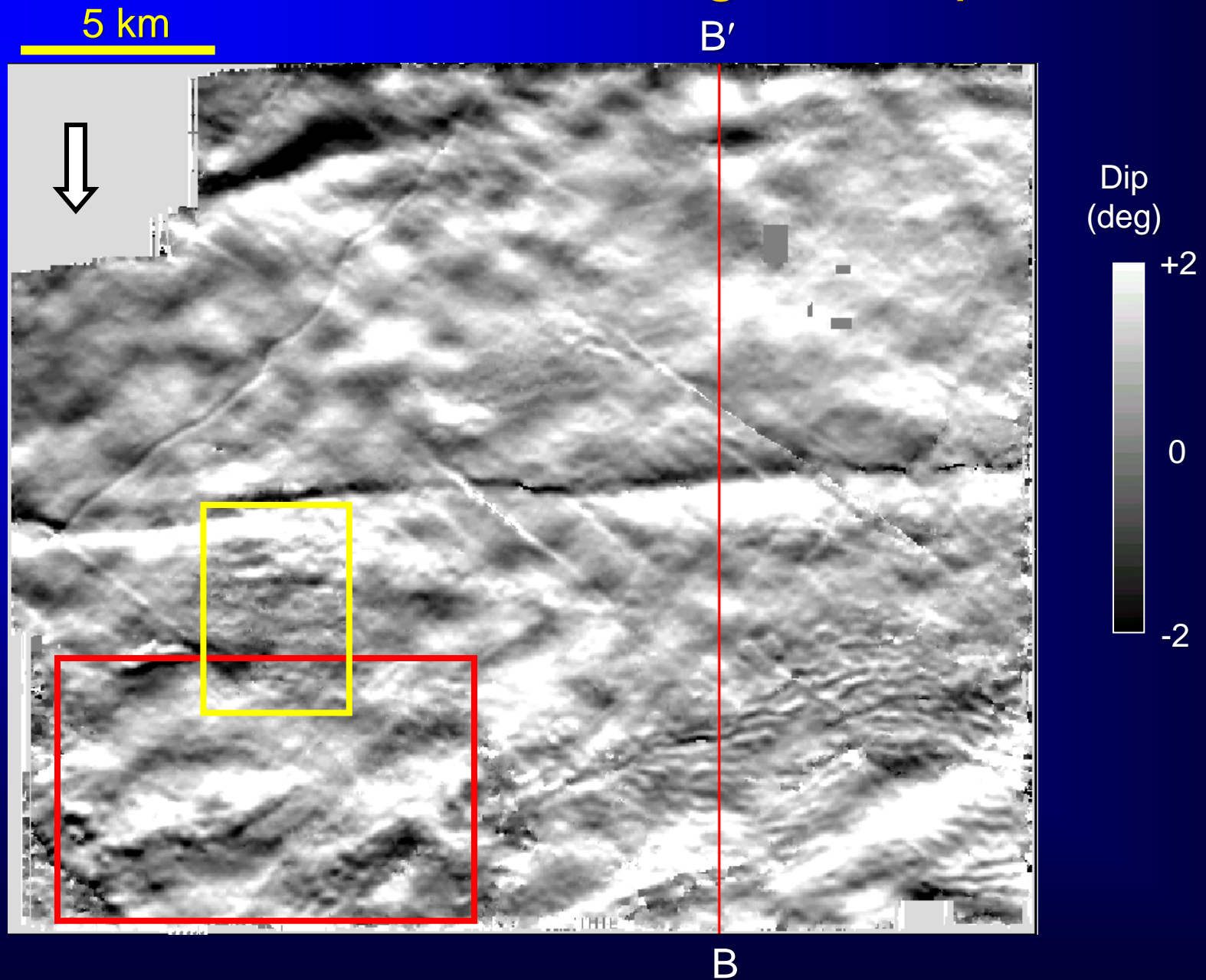
5 km

B'

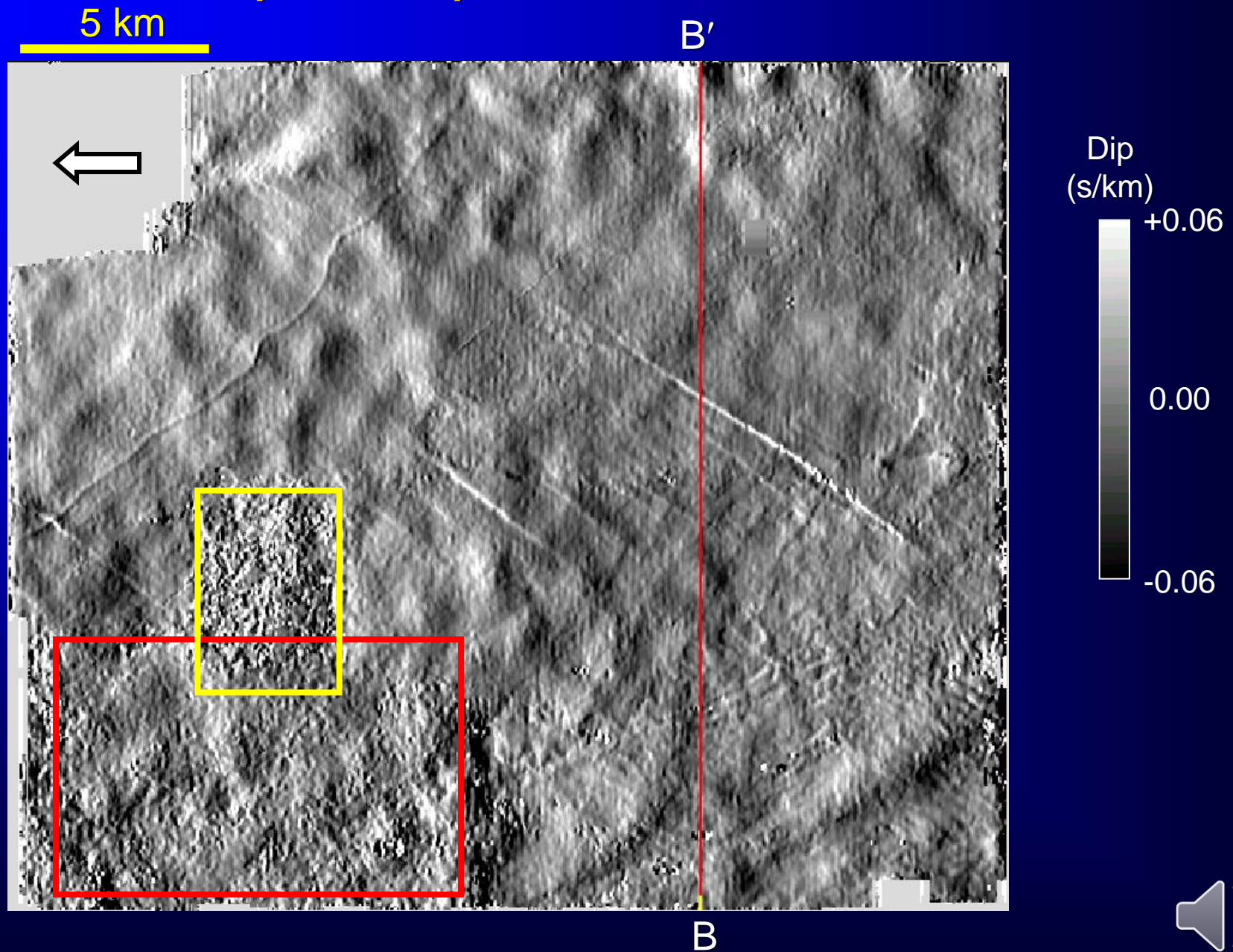




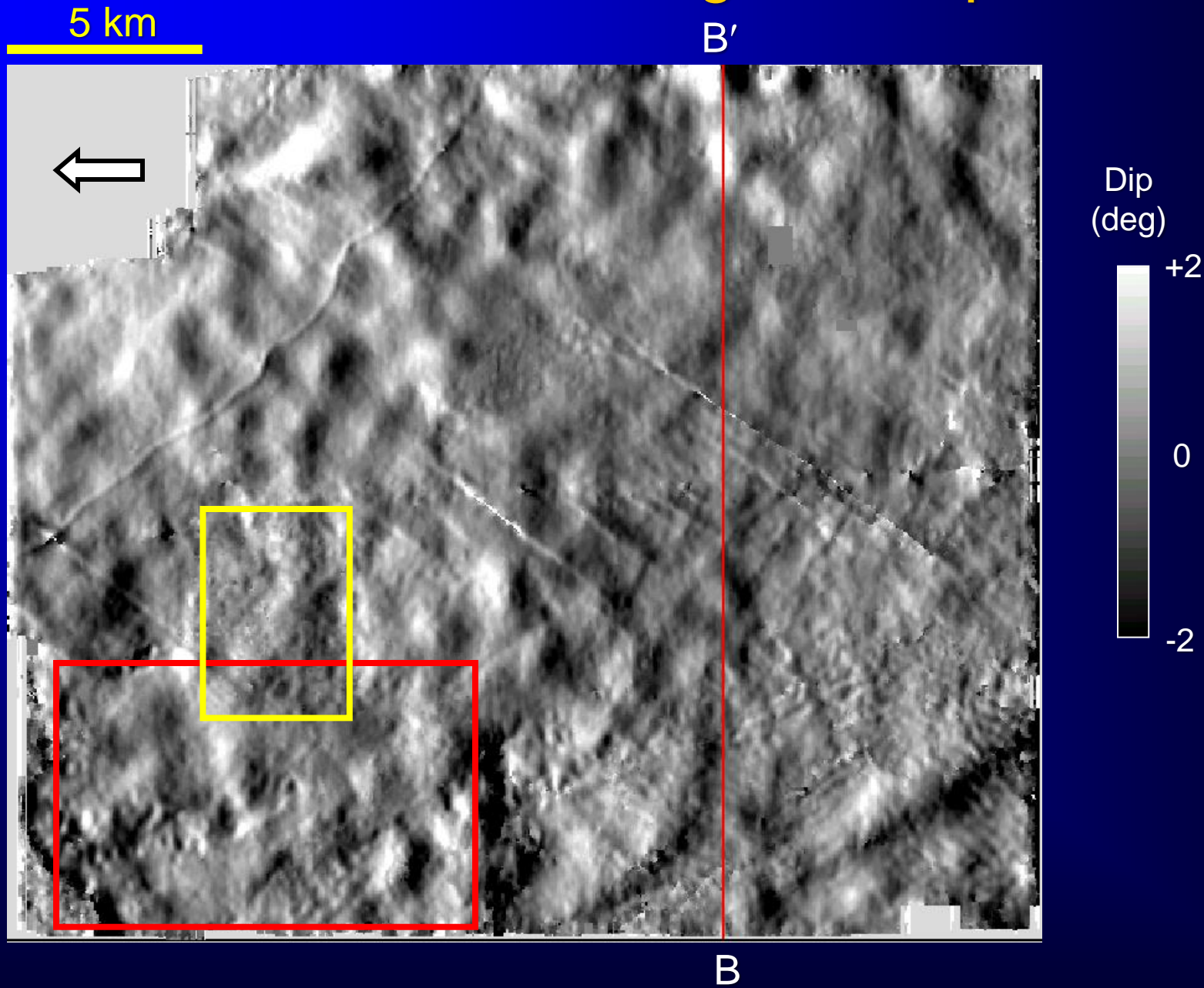
# Caddo horizon slice through NS dip volume



# EW dip from picked Caddo horizon

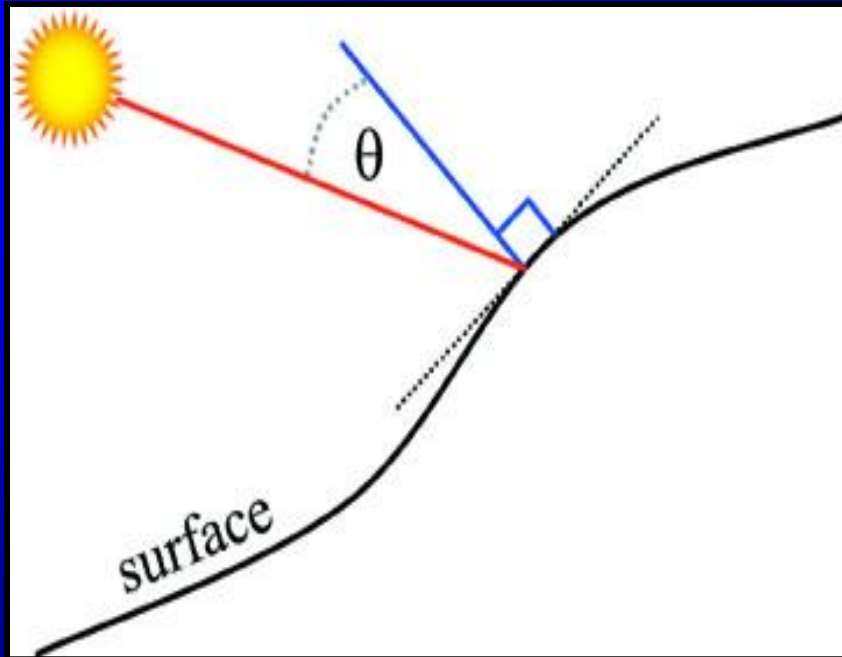


# Caddo horizon slice through EW dip volume

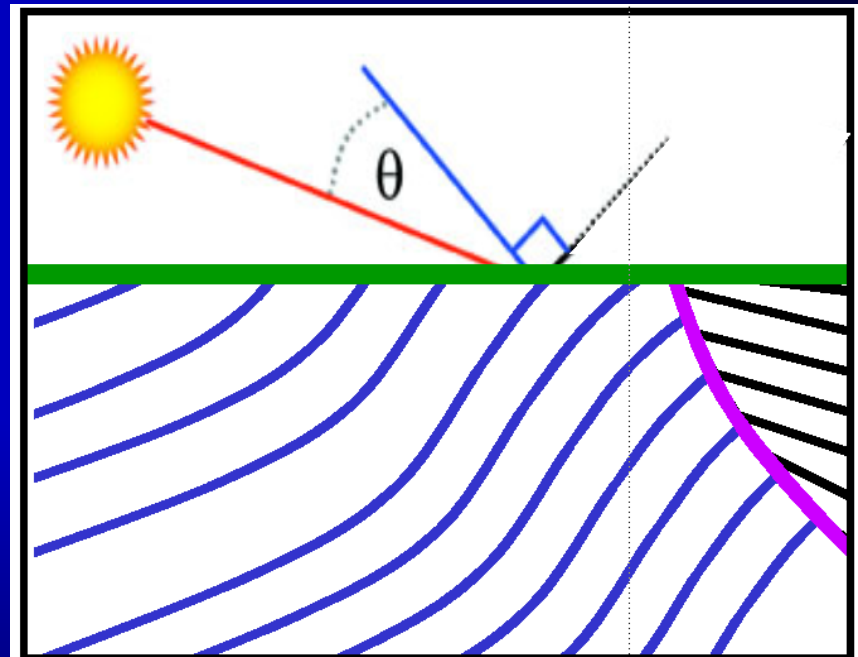




# Shaded illumination



on a surface

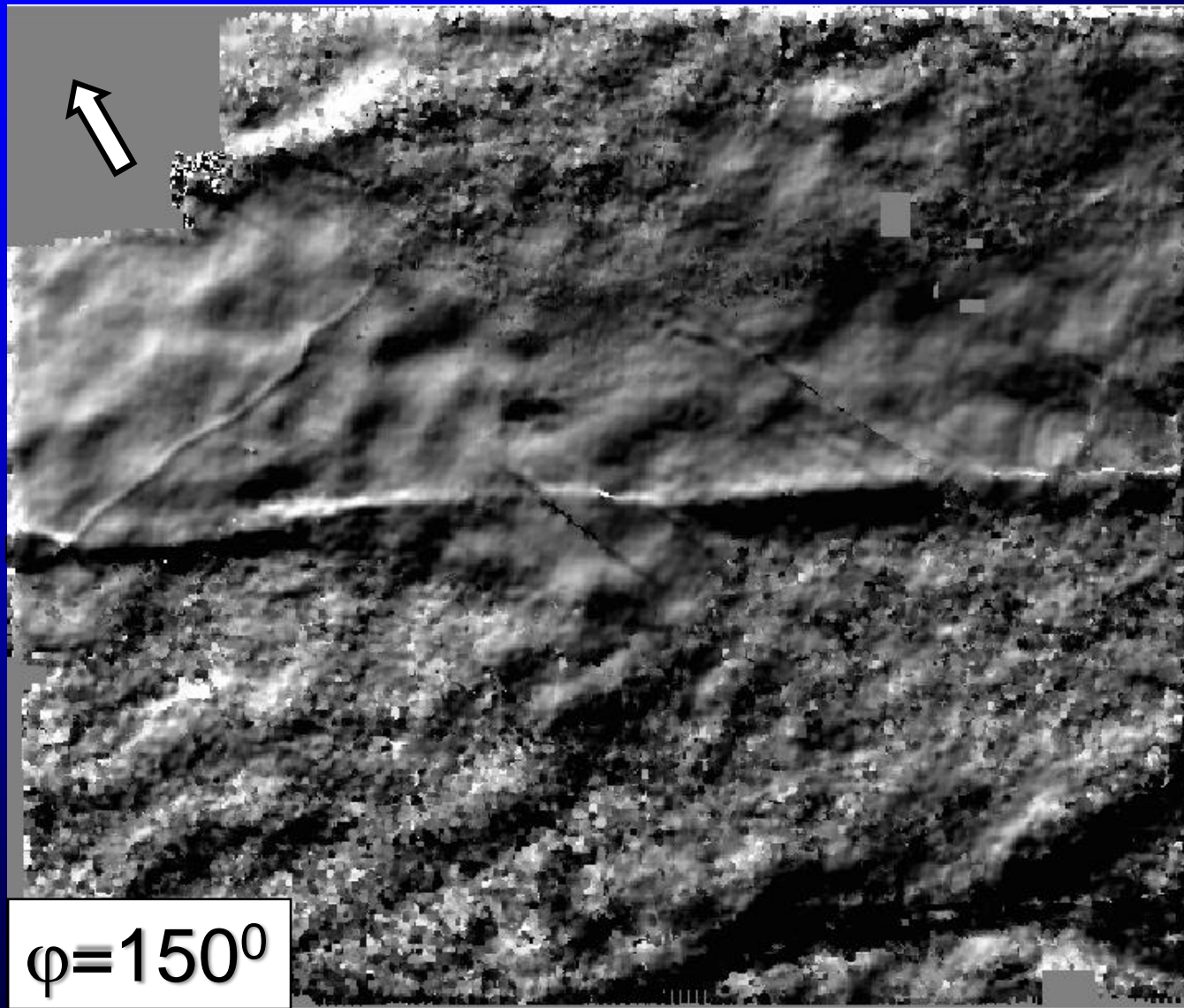


on a time slice through  
dip and azimuth volumes



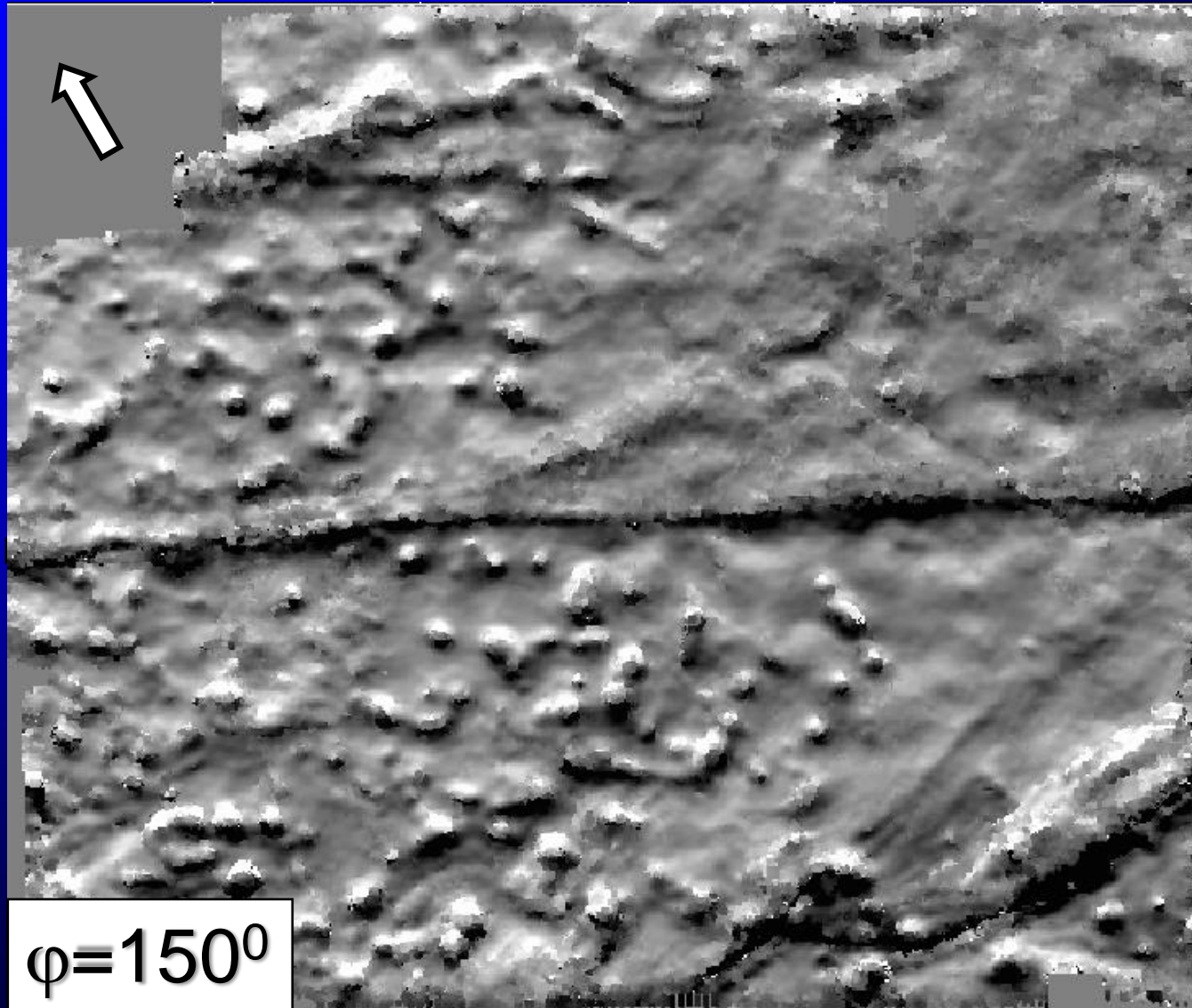
# Time slices through apparent dip (t=0.8 s)

5 km



# Time slices through apparent dip (t = 1.2 s)

5 km



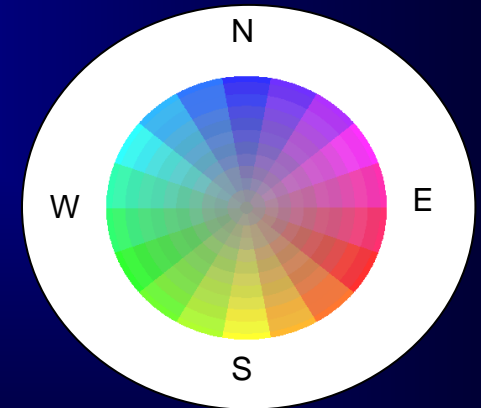
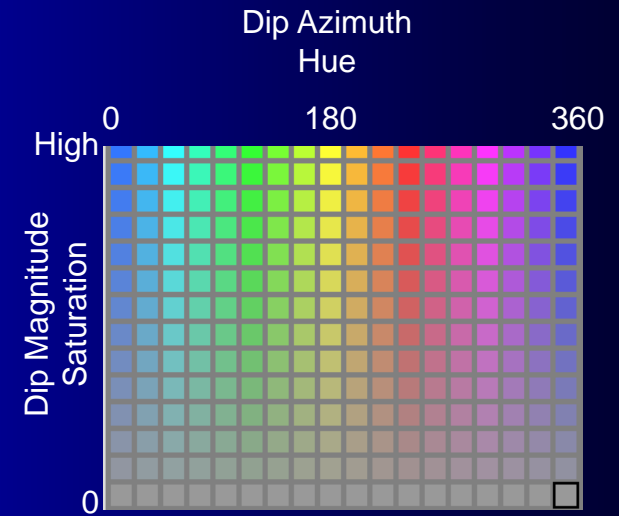
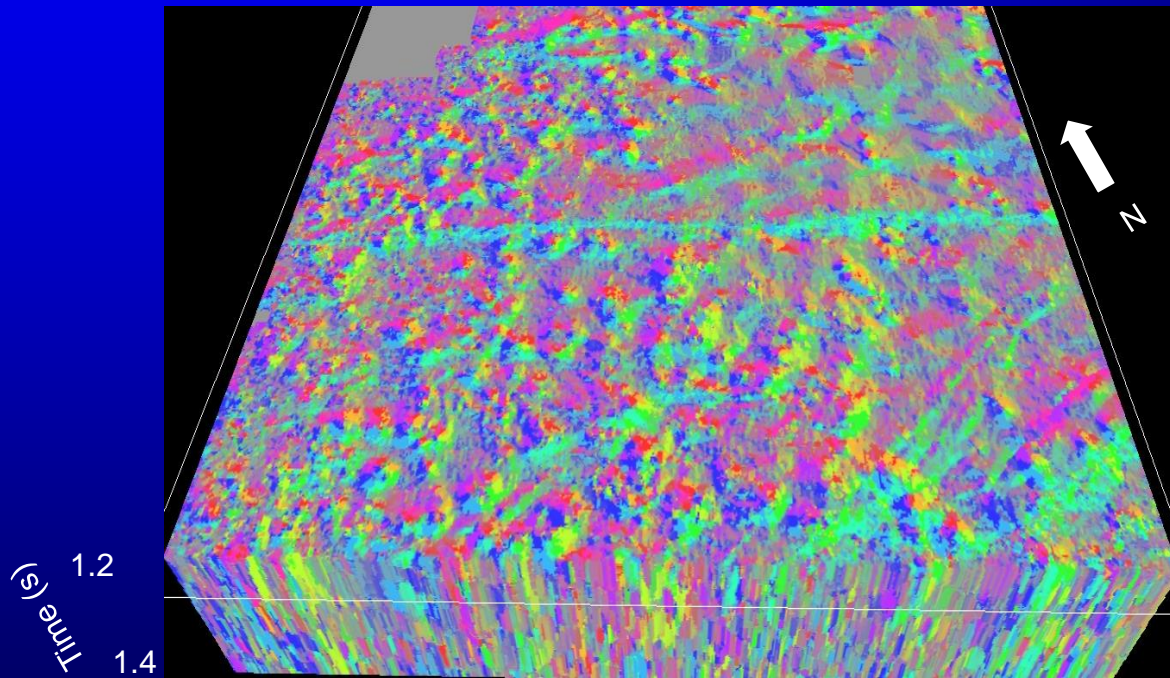
$\phi = 150^\circ$

Dip (deg)  
+2  
0  
-2





# Volumetric visualization of reflector dip and azimuth

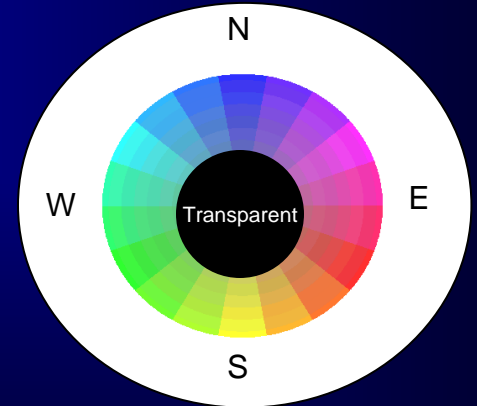
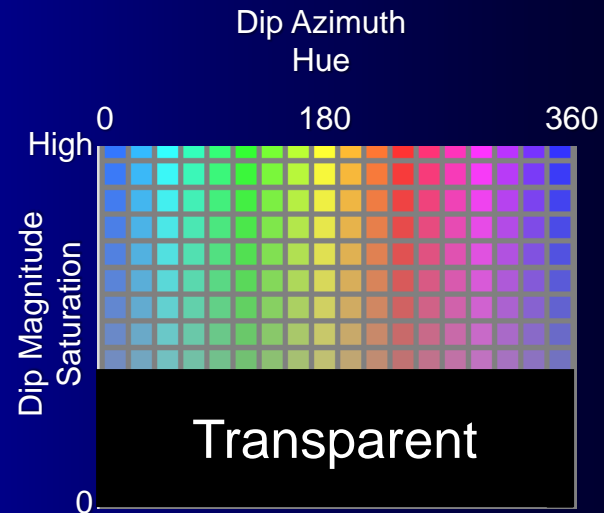
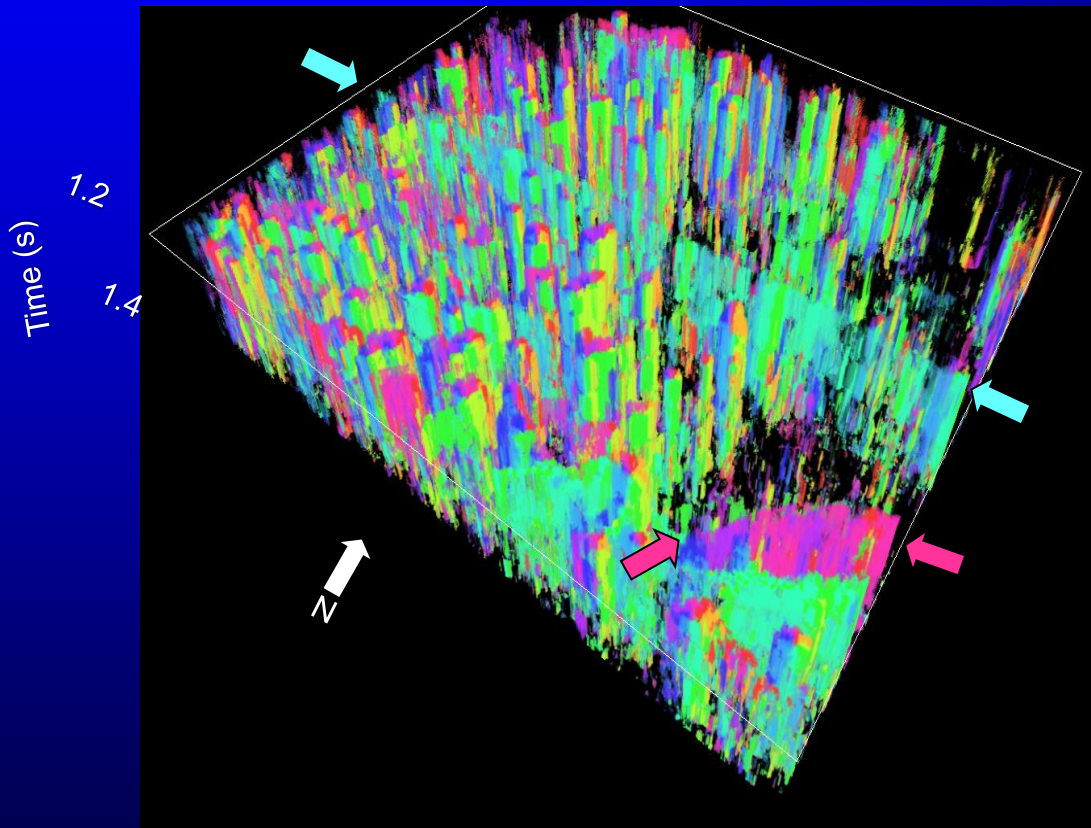


(c)



(Guo et al., 2008)

# Volumetric visualization of reflector dip and azimuth



(c)



(Guo et al., 2008)

# Volumetric Dip and Azimuth

## In Summary:

- Dip and azimuth estimated using a vertical window in general provide more robust estimates than those based on picked horizons
- Dip and azimuth volumes form the basis for volumetric curvature, coherence, amplitude gradients, seismic textures, and structurally-oriented filtering
- Dip and azimuth are the key components for computer-aided 3D seismic stratigraphy
- Dip and azimuth will suffer from fault shadow and other velocity pull-up and push-down artifacts

